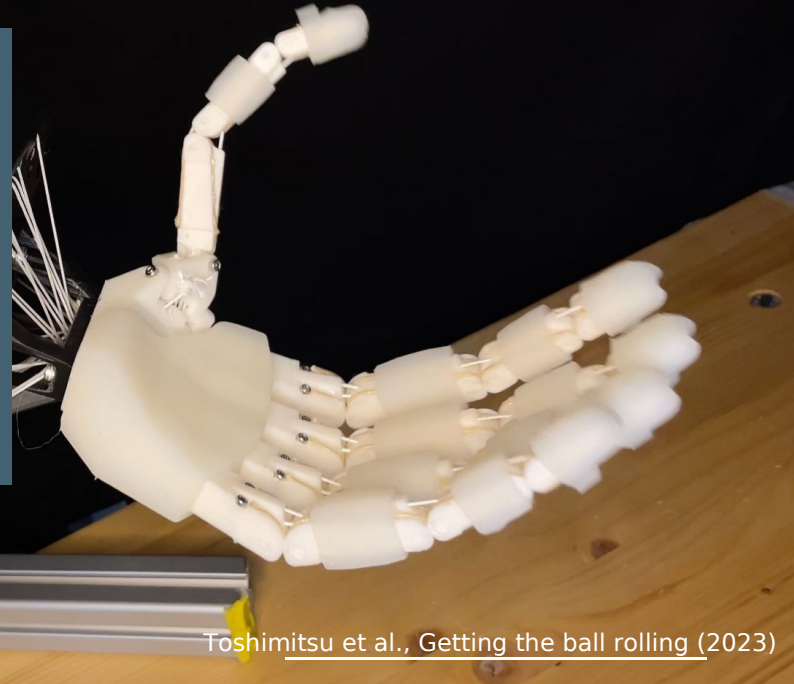




Implementing Control Strategies for Manipulation

Robert Katzschmann

Assistant Professor of Robotics, Soft Robotics Lab

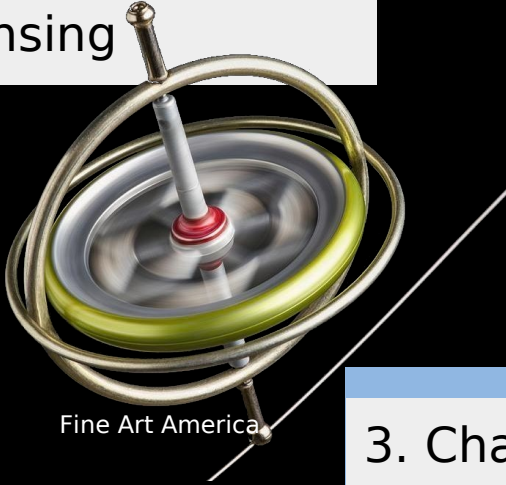


Toshimitsu et al., Getting the ball rolling (2023)



Plan for Today

1. Sensing



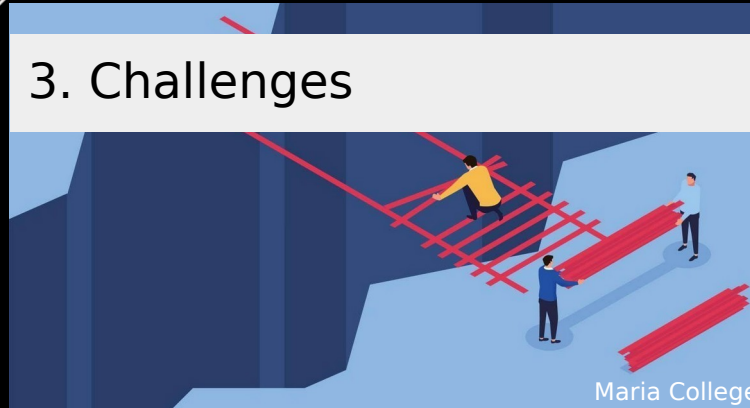
Fine Art America

2. Control



Wikimedia

3. Challenges

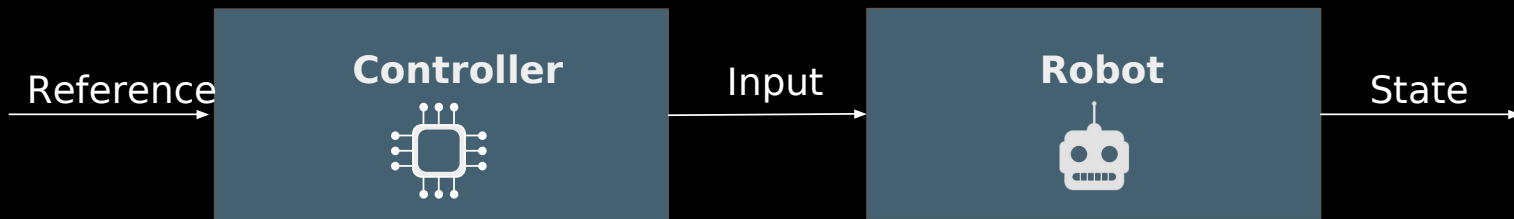


Maria College

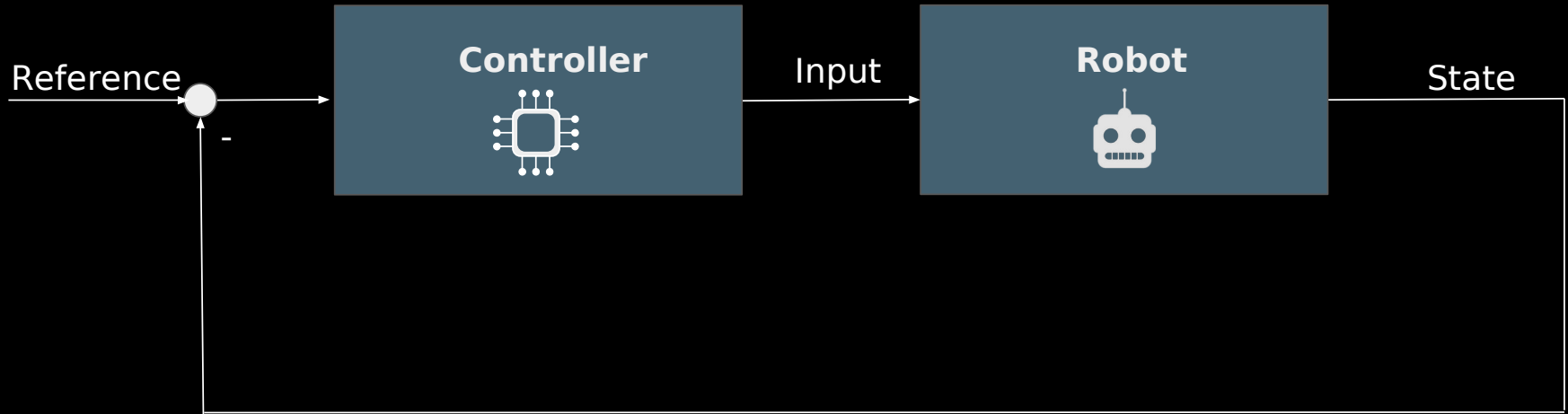


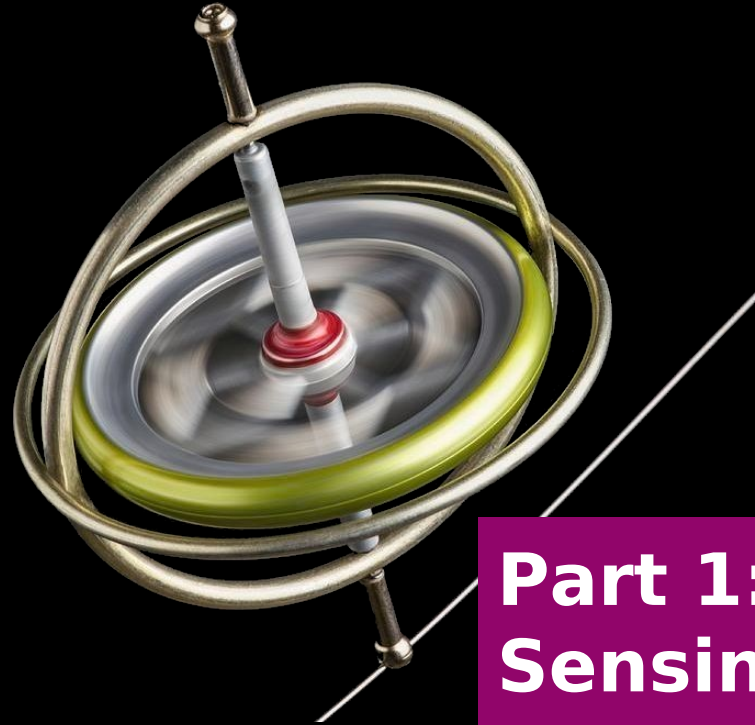
Control, but how?

Simplest controller possible: Open loop



Closed Loop Controller





Part 1: Sensing

Fine Art America

Sensing the pose: two methods

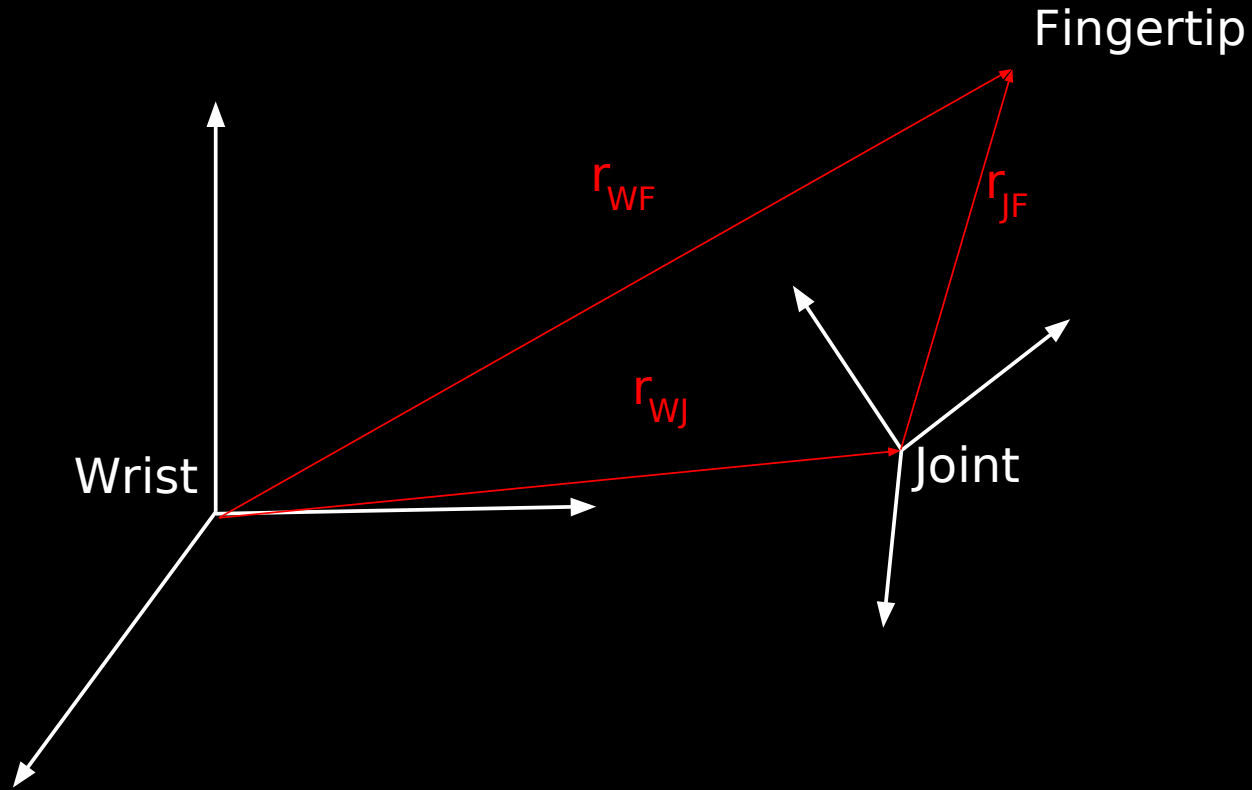


- **Direct** methods: Direct reference to the **world reference frame**
 - The sensors obtain the absolute value of the state we are measuring
- **Indirect** methods: Obtain a measurement with reference to a **second frame**
 - The sensors will estimate a relative measurement, that can be transformed into an absolute measurement





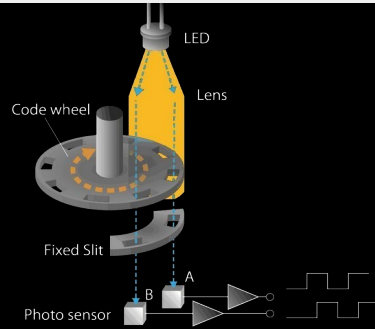
Second solution



What sensors you might find in the future?

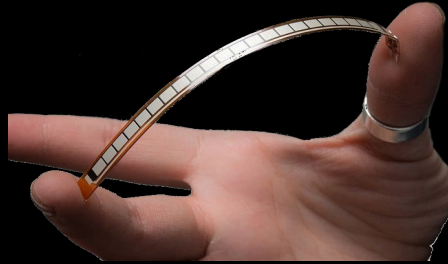


• Motor Encoders



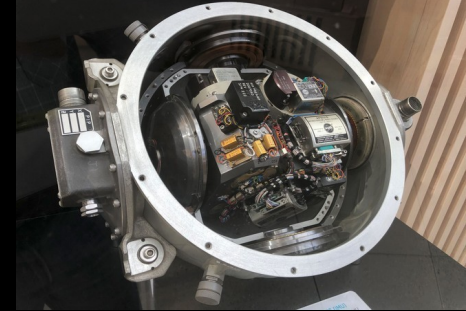
[Asahi Kasei Microdevices](#)

• Flex Sensors



[AdaFruit](#)

• IMU



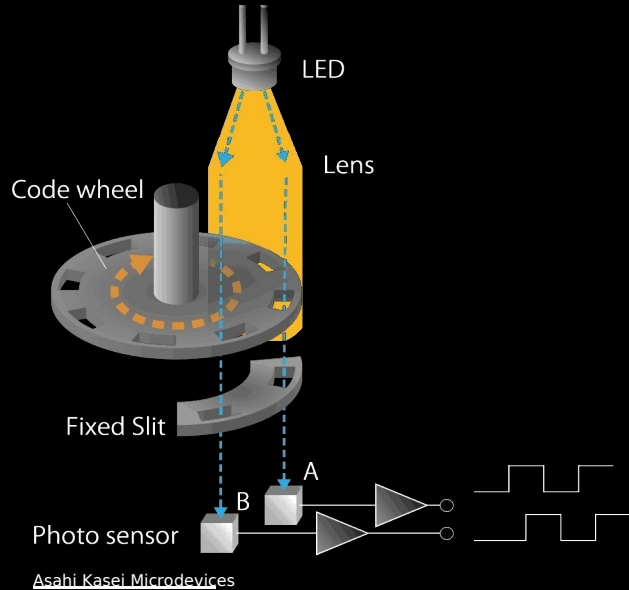
[Wikimedia](#)

• Other principles?



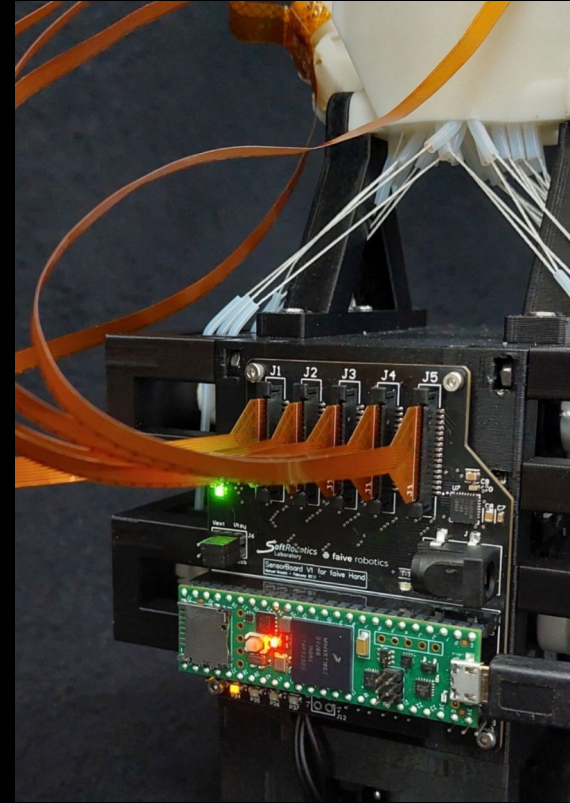


1. Encoders

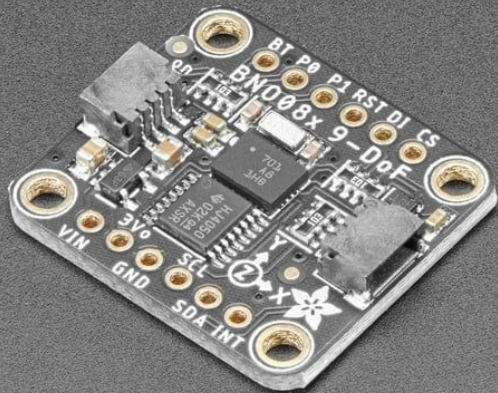




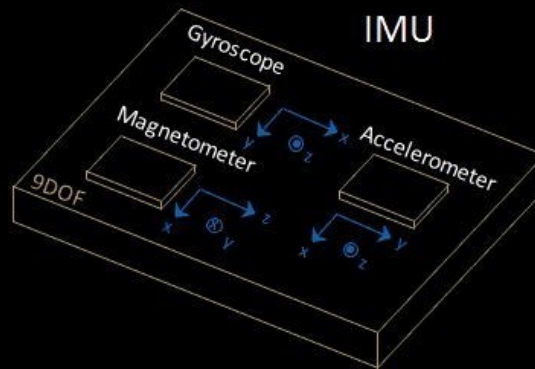
2. Flex Sensors



3. Inertial Measurement Unit

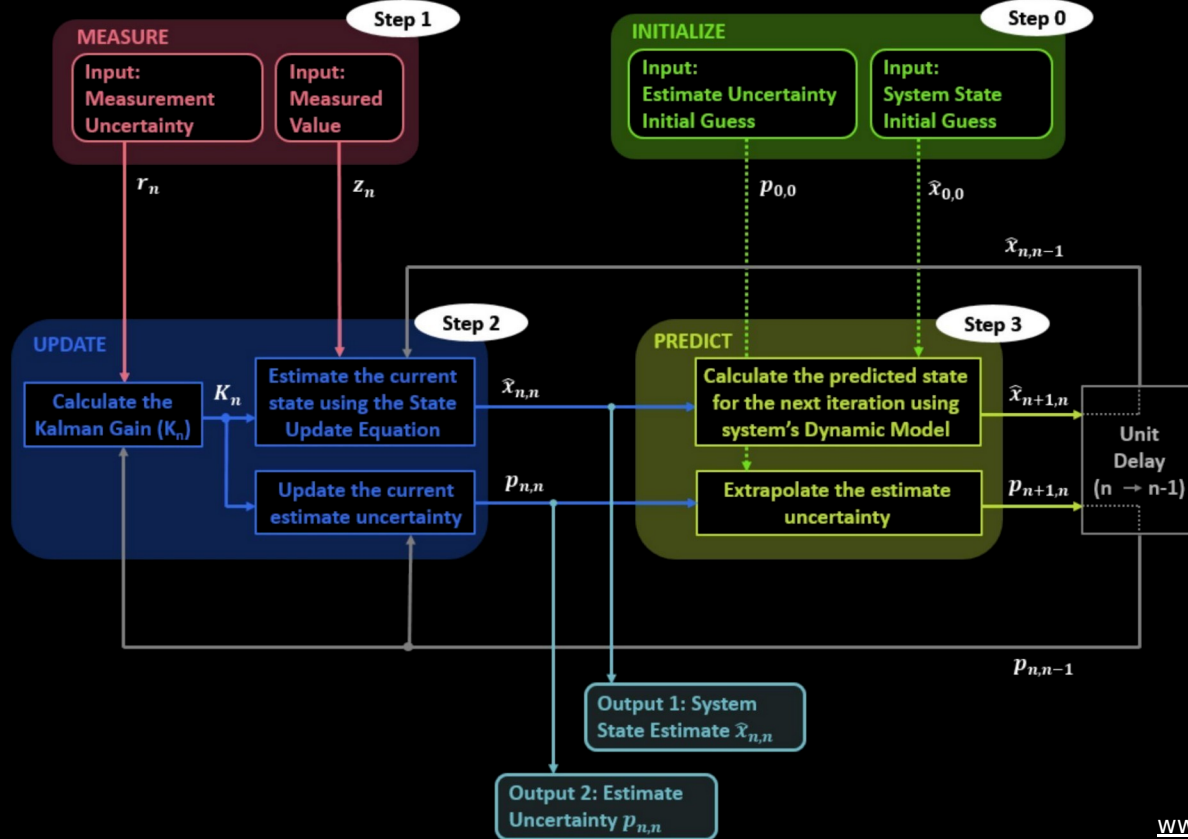


Adafruit



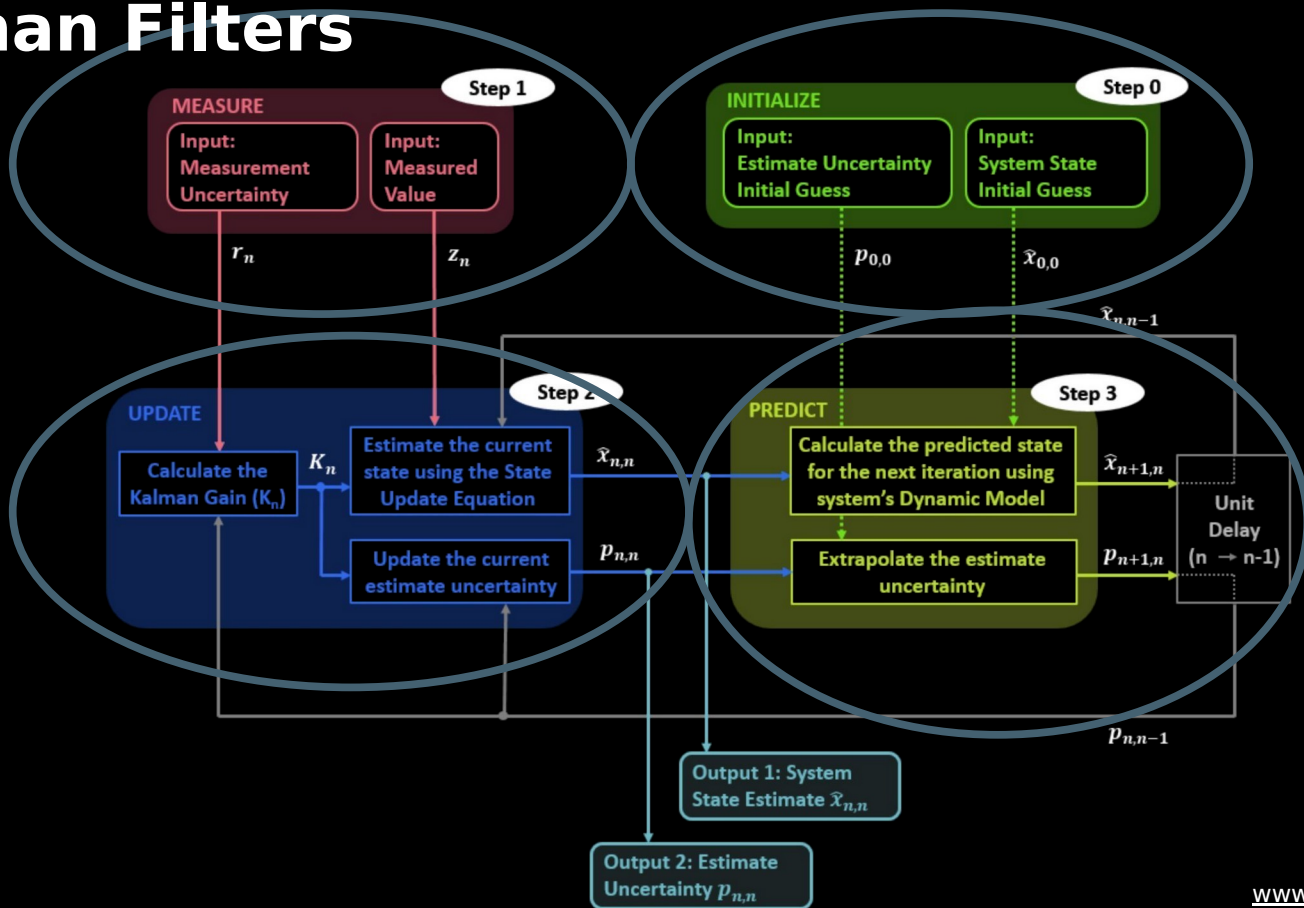
Mathworks

Kalman Filters





Kalman Filters





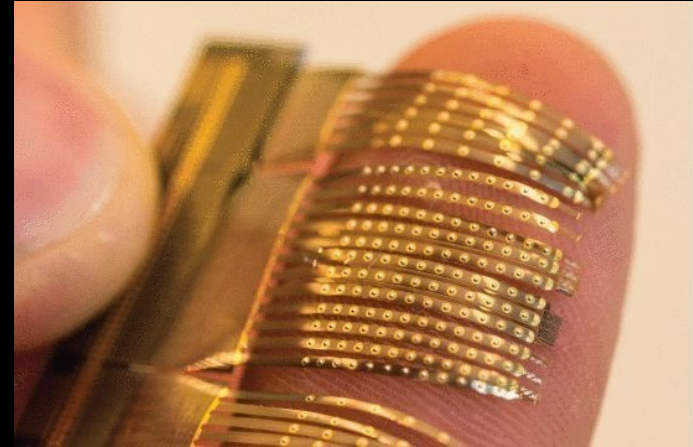
Sensing the touch:

- Force Sensing Resistors



Ohmite

- Artificial Skin

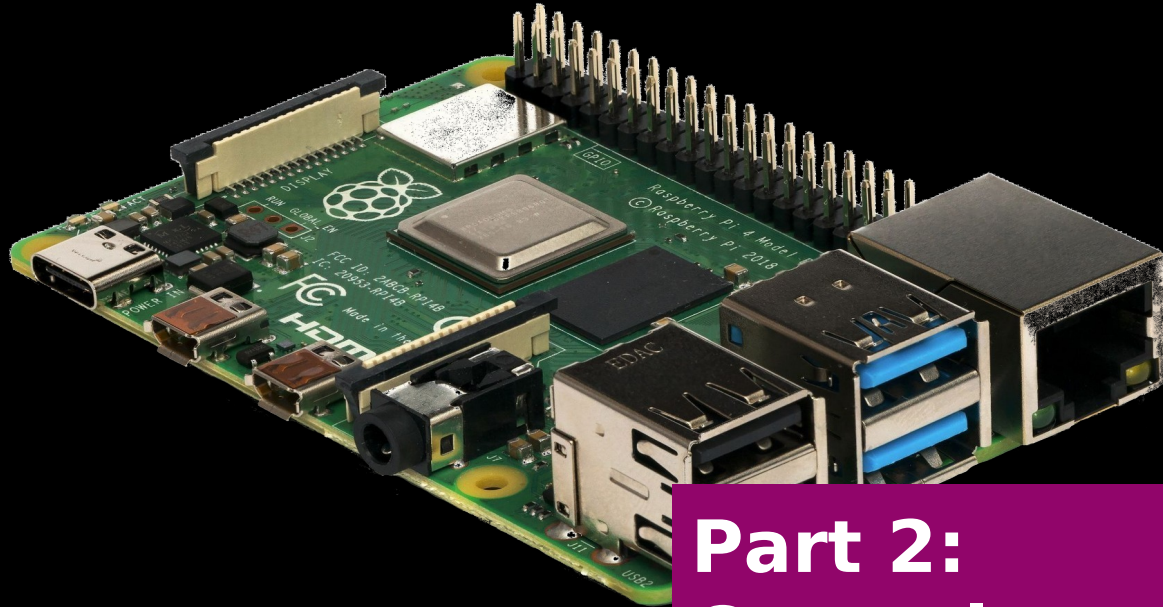


Weichart et al. *Tactile Sensing With Scalable Capacitive Sensor Arrays on Flexible Substrates* (2021)

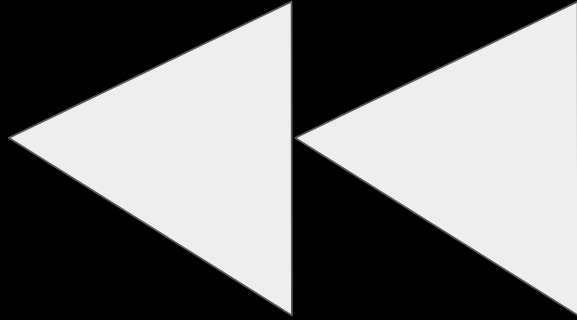


Wrapping up

- **Pose** estimation
 - Directly measuring the absolute pose (6 DoF)
 - Camera triangulation
 - Measuring the pose with respect to the wrist
 - Encoders
 - Flex sensors
 - Inertial Measurement Unit
 - Kalman Filters
- **Force** estimation
 - Force Sensing Resistors
 - Artificial Skin



Part 2: Control





Inverse Kinematics

- From greek **kinema** = motion
- In the past units we learnt that:
 - $J(q)\dot{q} = \chi_e = \begin{bmatrix} \dot{p}_e \\ w_e \end{bmatrix}$
- If we invert it we obtain:
 - $\dot{q} = J^+ \chi_e$ with $J^+ = J^T (J J^T)^{-1}$
- And in a differential form:
 - $\Delta \chi_e = J^+ \Delta q$

Algorithm 1 Numerical Inverse Kinematics

```

1:  $\mathbf{q} \leftarrow \mathbf{q}^0$  ▷ Start configuration
2: while  $\|\chi_e^* - \chi_e(\mathbf{q})\| > tol$  do ▷ While the solution is not reached
3:    $\mathbf{J}_{eA} \leftarrow \mathbf{J}_{eA}(\mathbf{q}) = \frac{\partial \chi_e}{\partial \mathbf{q}}(\mathbf{q})$  ▷ Evaluate Jacobian for  $\mathbf{q}$ 
4:    $\mathbf{J}_{eA}^+ \leftarrow (\mathbf{J}_{eA})^+$  ▷ Calculate the pseudo inverse
5:    $\Delta \chi_e \leftarrow \chi_e^* - \chi_e(\mathbf{q})$  ▷ Find the end-effector configuration error vector
6:    $\mathbf{q} \leftarrow \mathbf{q} + \mathbf{J}_{eA}^+ \Delta \chi_e$  ▷ Update the generalized coordinates
7: end while

```

A possible inverse kinematics algorithm

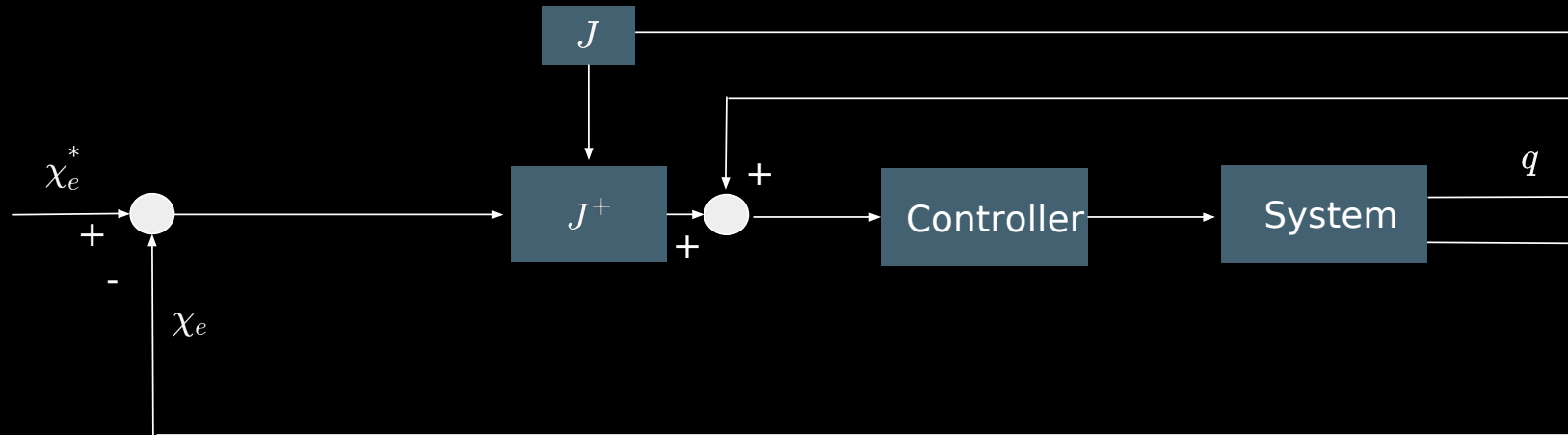
Marco Hutter, Roland Siegwart
Robot Dynamics Class ETH

To overcome stability issues the update can be scaled by a factor k

$$q \leftarrow q + k J_{eA}^+ \Delta \chi_e \text{ with } k \in (0, 1)$$

However this leads to a slower convergence

Inverse Kinematics



Trajectory Control



We can use a closed loop controller, but we need to add a component for the desired velocities

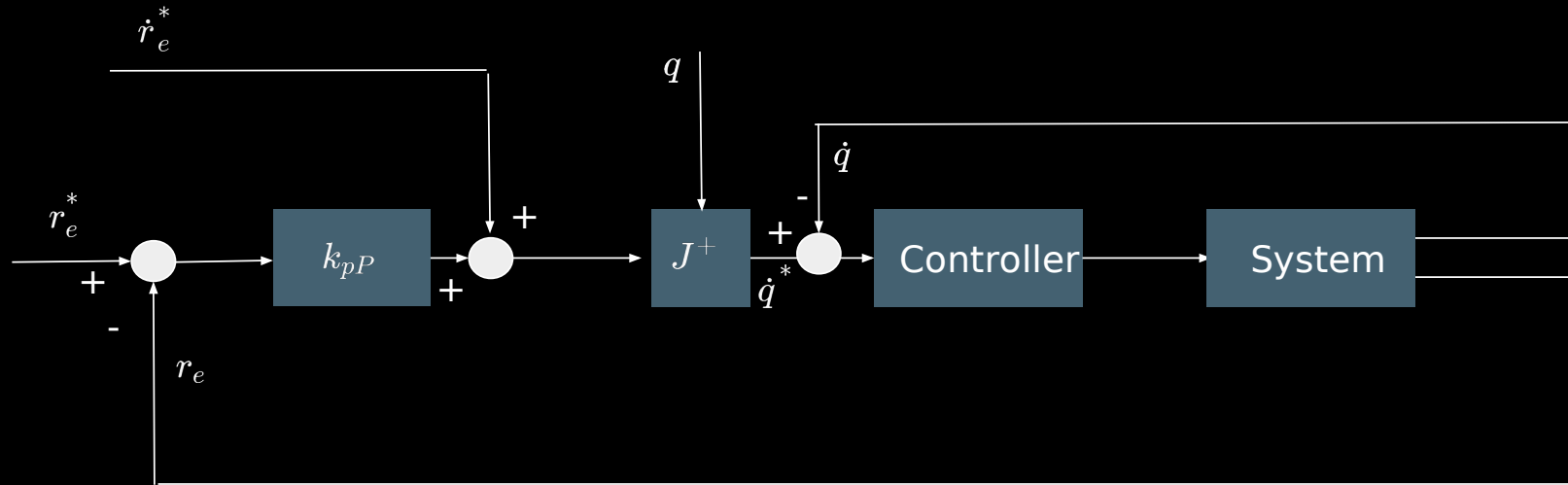
We define $\Delta r_e^t = r_e^*(t) - r_e(q^t)$

And the desired joint velocity $\dot{q}^* = J_{e0P}^+(q^t) \cdot (\dot{r}_e^*(t) + k_{pP} \Delta r_e^t)$

If we have a desired rotation rate we write $\dot{q}^* = J_{e0R}^+(q^t) \cdot (\omega_e^*(t) + k_{pR} \Delta \phi)$

Where ϕ are the angles used to represent the orientation of the end effector.

Trajectory Control





Dynamic control

The dynamic model is

$$M(q)\ddot{q} + b(q, \dot{q}) + g(q) = \tau + J_c(q)^T F_c$$

With:

$M(q)$: Generalized mass matrix

q, \dot{q}, \ddot{q} : Generalized position, velocity and acceleration vector

$b(q, \dot{q})$: Coriolis and centrifugal terms

$g(q)$: Gravitational terms

τ : External generalized forces

F_c : External Cartesian forces

$J_c(q)$: Geometric Jacobian corresponding to the external forces



Dynamic control

The dynamic model is

$$M(q)\ddot{q} + b(q, \dot{q}) + g(q) = \tau + J_c(q)^T F_c$$

If we know the desired generalized accelerations, velocities and poses we can write

$$\ddot{q}^* = k_p(q^* - q) + k_d(\dot{q}^* - \dot{q})$$

Thus the joint torques will be

$$\tau^* = M(q)\ddot{q}^* + b(q, \dot{q}) + g(q)$$



Task-space control

Remember that $J(q)\dot{q} = \chi_e = \begin{bmatrix} \dot{p}_e \\ w_e \end{bmatrix}$

If you derive that with respect to time $\dot{\chi}_e = J(q)\ddot{q} + \dot{J}(q)\dot{q}$

And if we solve the dynamics equation for the joint acceleration and substitute in the equation above get: $\dot{\chi}_e = JM^{-1}(\tau - b - g) + \dot{J}\dot{q}$

Finally, remembering that $\tau = J_e^T F_e$

We can write $\Lambda_e \dot{\chi}_e + \mu + p = F_e$

$$\begin{aligned} \Lambda_e &= (J_e M^{-1} J_e^T)^{-1} \\ \mu &= \Lambda_e J_e M^{-1} b - \Lambda_e \dot{J}_e \dot{q} \\ p &= \Lambda_e J_e M^{-1} g \end{aligned}$$



Task-space control

Defining the dynamics uniquely depending on the state of the end effector allows us to design a control loop

$$\dot{\chi}_e^* = \begin{pmatrix} r_e^* - r_e \\ \Delta\phi_e \end{pmatrix} + k_d(\chi_e^* - \chi_e)$$



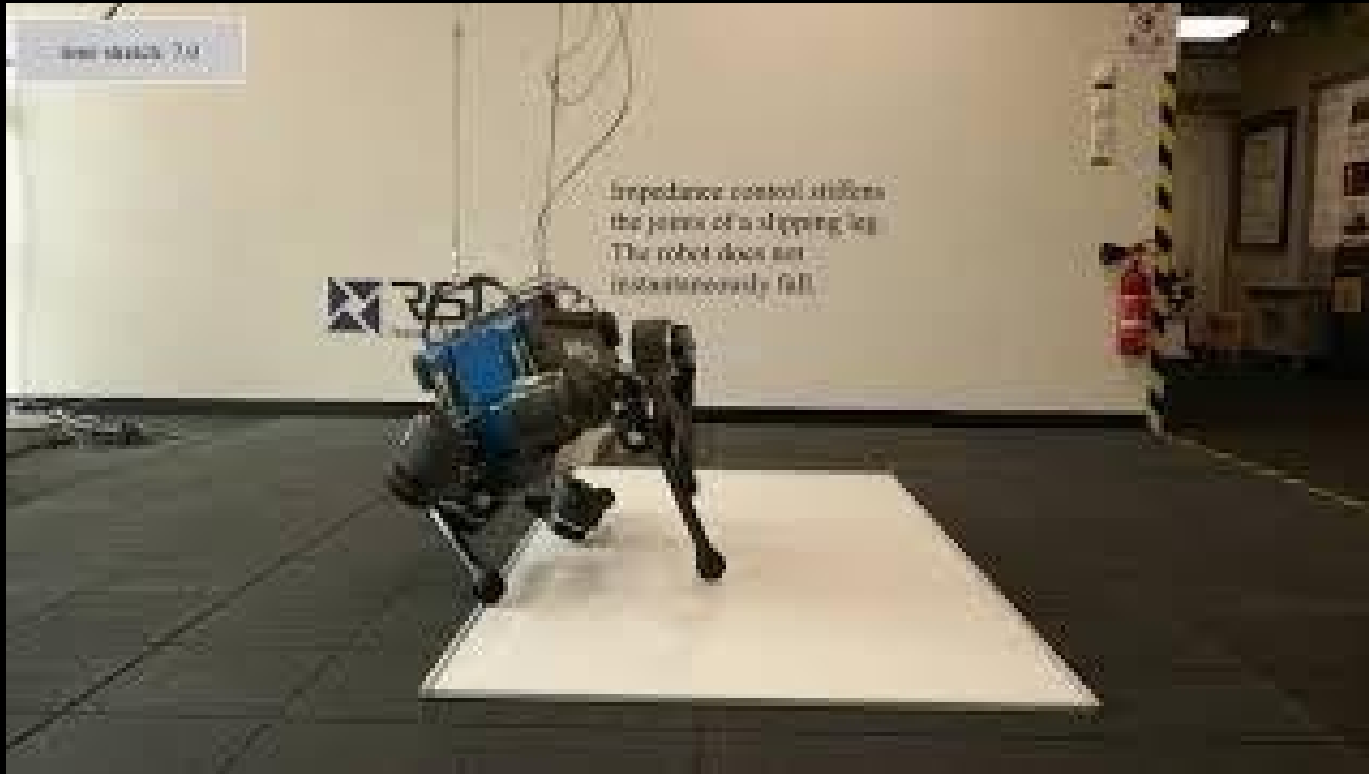
Part 3: Challenges



What should you expect?

- Uncertainty and Partial Observability
- Long Horizon
- Under/Over actuation
- Sim-to-real gap
- Tendon strain
- Skin non-linearity
- Encoder's sensibility

Uncertainty and Partial Observability



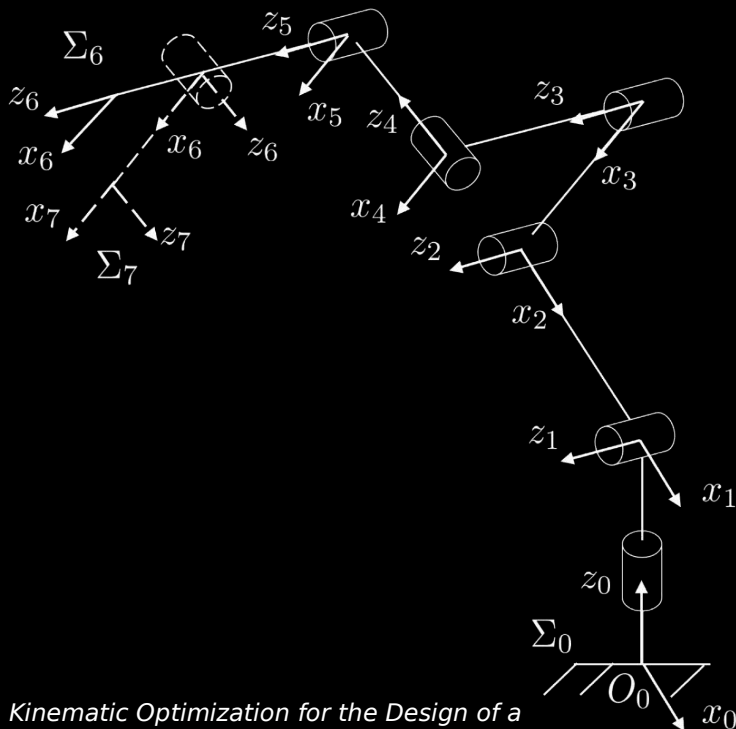
Long Horizon



Thyssenkrupp X Embotech

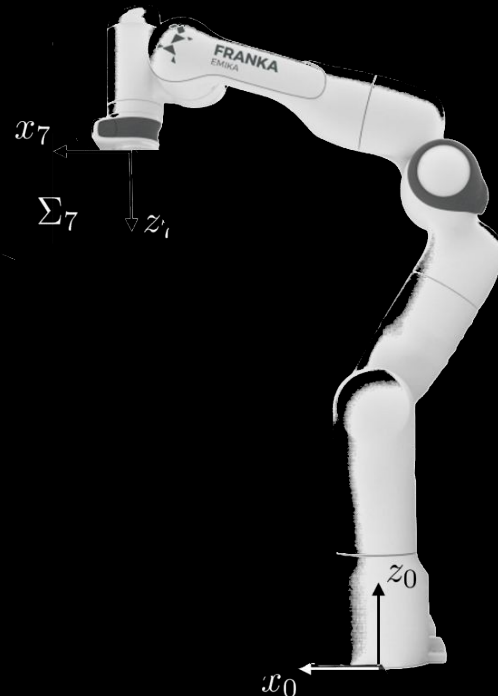


Underactuation and Overactuation



(a)

Filippeschi et al. *Kinematic Optimization for the Design of a Collaborative Robot End-Effector for Tele-Echography* (2021)

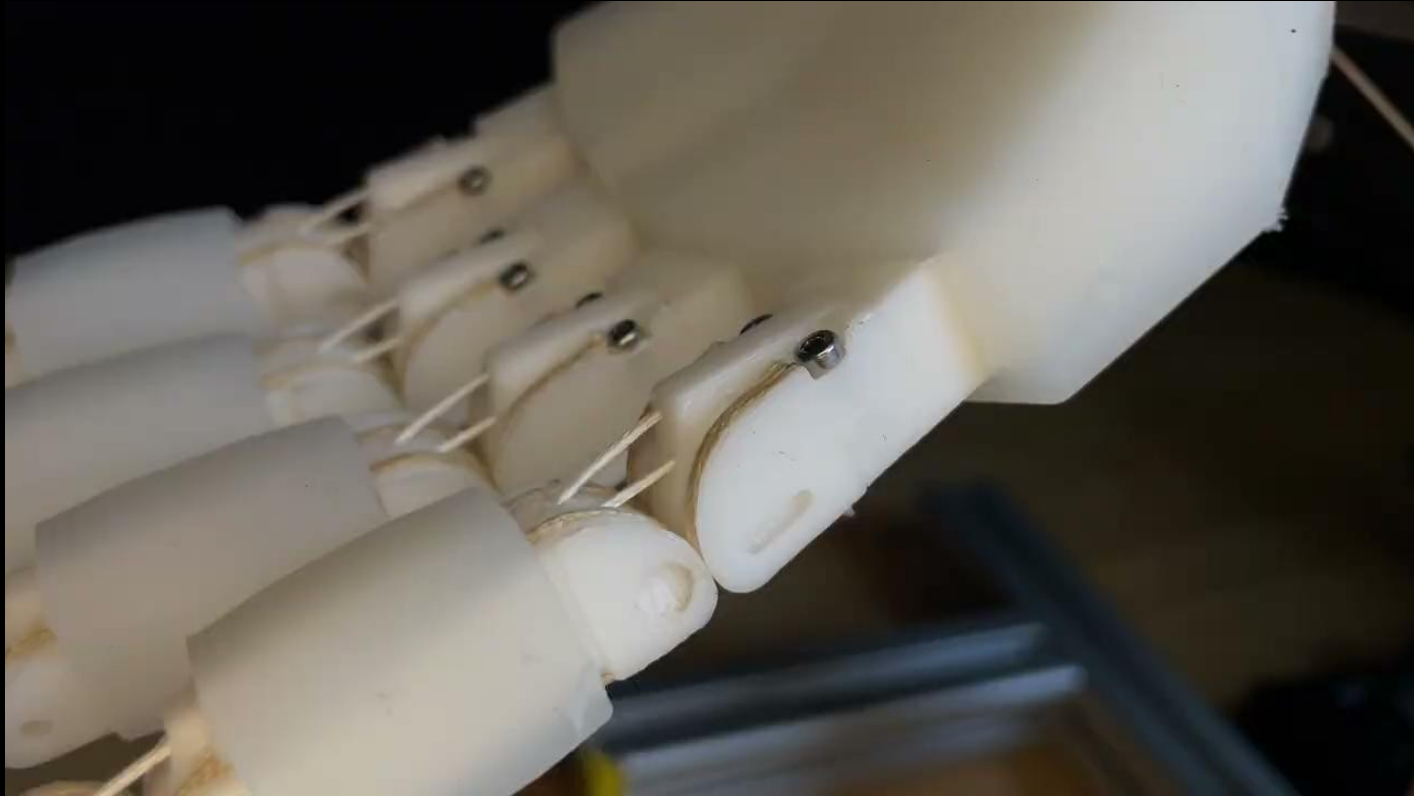


(b)

Sim-to-real gap

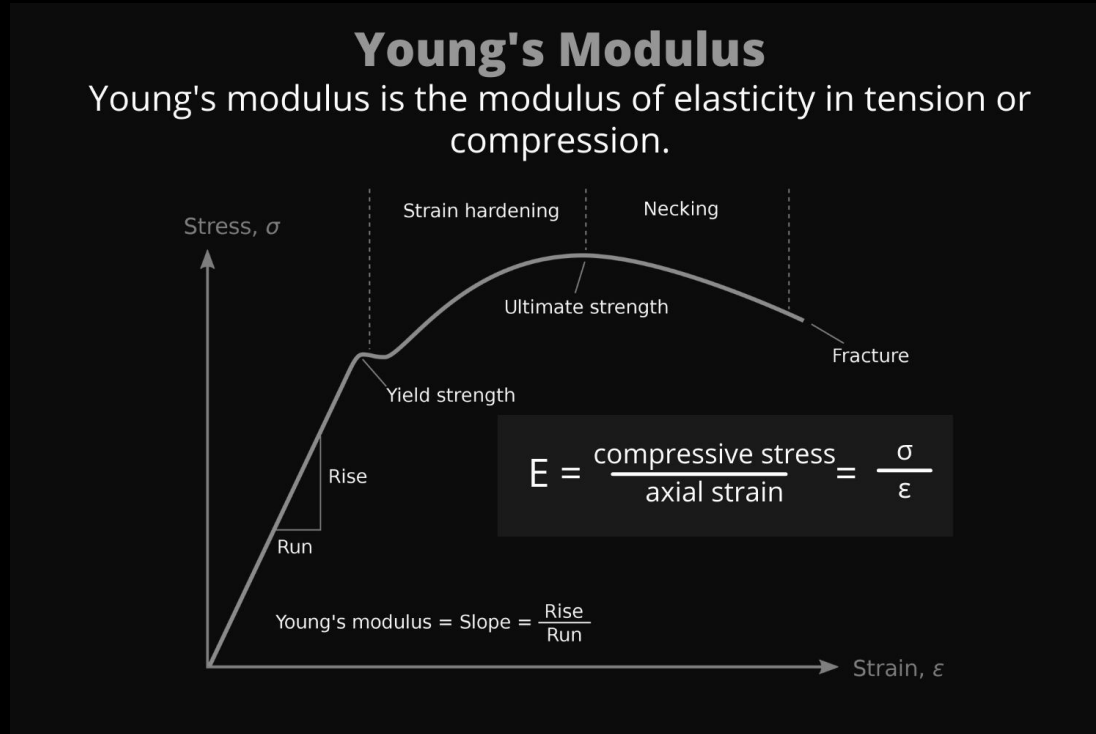


Tendon strain





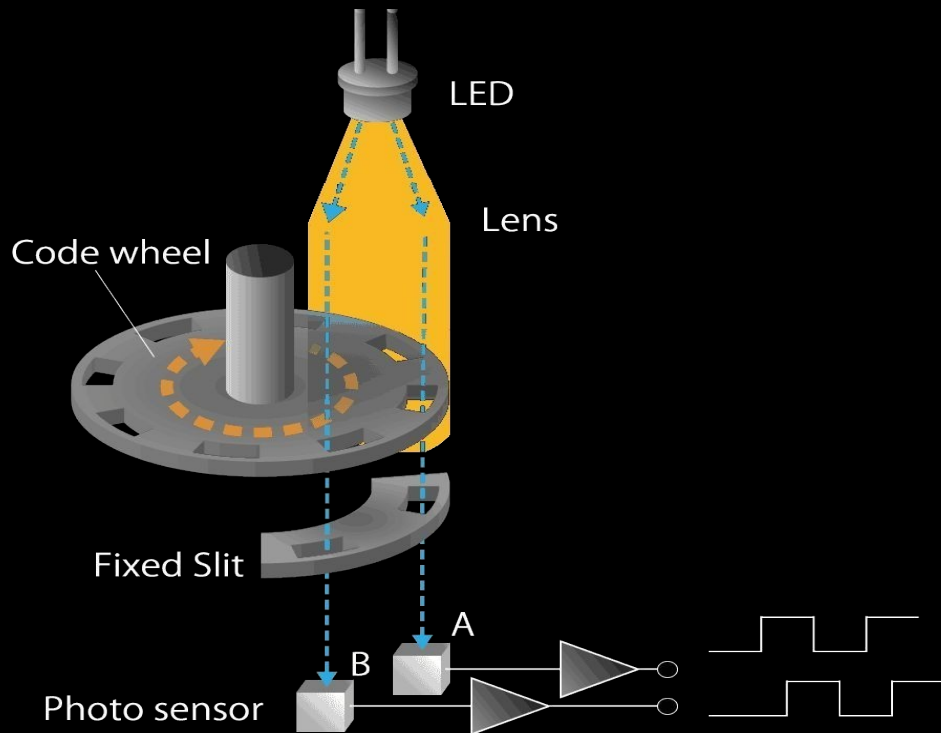
Soft non-linearity: example



Science Notes



Encoder's uncertainty: example

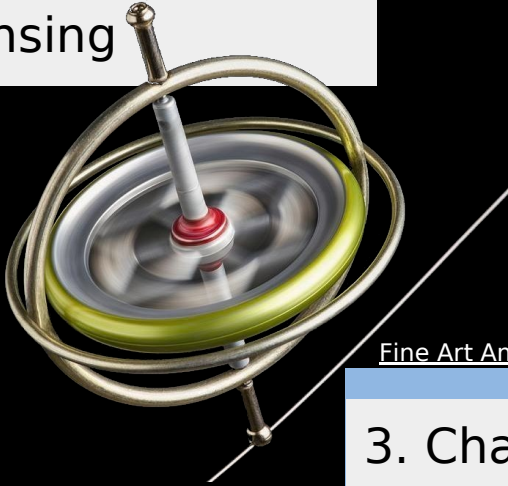


Asahi Kasei Microdevices

Let's wrap up



1. Sensing



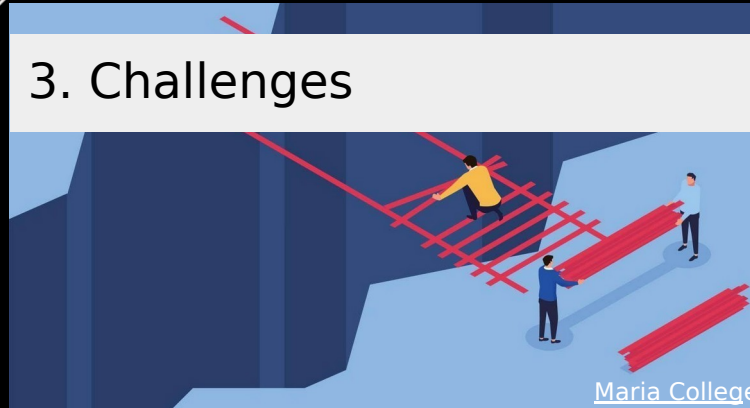
2. Control



[Fine Art America](#)

[Wikimedia](#)

3. Challenges



[Maria College](#)

Useful links



<https://link.springer.com/book/10.1007/978-3-319-54413-7>

<https://smartlabai.medium.com/a-brief-overview-of-imitation-learning-8a8a75c44a9c>

<https://underactuated.csail.mit.edu/index.html>

<https://www.kalmanfilter.net/default.aspx>