











	17 Nov	24 Nov	1 Dec
	Imitation Learning	Guest Lecture	Product Development
14:15-15:00	Davide Liconti	Oier Mees @ Microsoft Spatial Al Lab	Benedek Forrai @ Mimic Robotics
15:15-16:00	Training Policies with SRL_IL (workshop)	VLAs and Foundation Models	Class Wrap-up and Q&A
	Chenyu Yang	Davide Liconti	Robert Katzschmann

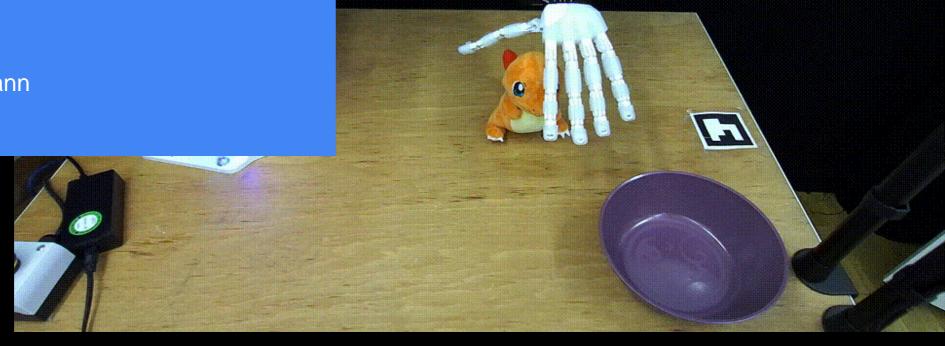






# **Imitation learning**

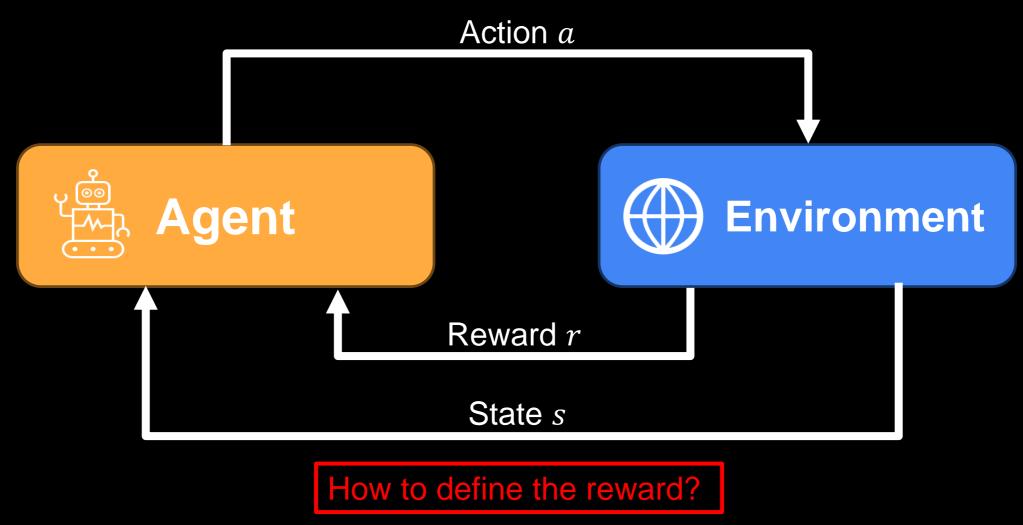
Davide Liconti Prof. Robert Katzschmann 17 November 2025





# Reinforcement Learning (RL) Recap



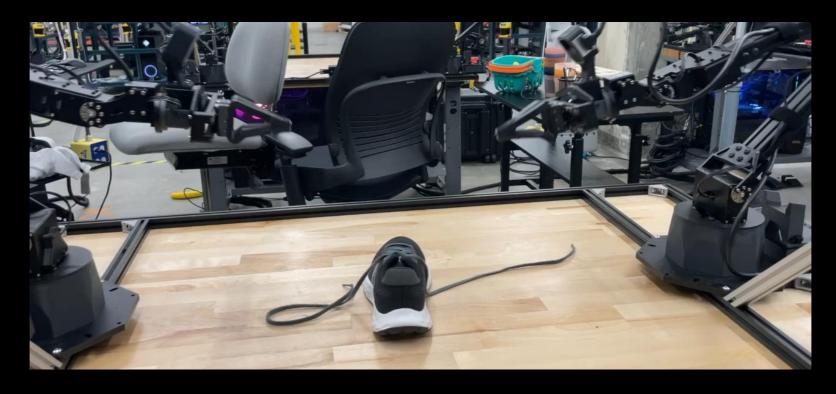






### What's the reward function for this task?





- Sparse reward: +1 when tied (RL won't explore enough).
- Dense reward: but what is the distance to "tiedness"?
- Multi-step, long-horizon manipulation → reward shaping quickly becomes arbitrary or impossible.

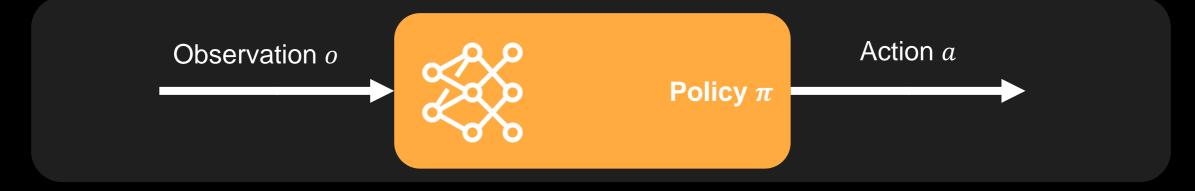




### **Imitation Learning (IL)**



aka Behavior Cloning (BC), aka Learning from Demonstrations (LfD)





Given a dataset of "Expert transitions"

$$\mathfrak{D} = \{(o_t, a_t)\}_{t=1}^N$$

Simple supervised regression :  $\pi = \arg \min \mathbb{E}_{(o,a) \sim \mathfrak{D}} [\|a - \pi(o)\|^2]$ 

How to collect data? → previous lecture





# **Imitation Learning (IL)**

### why does it dominate today

Today IL is by far the dominant approach for manipulation

- No complex or arbitrary reward shaping
- No sim2real gap (for real world teleop data)
- Simpler, easier to debug and interpret
- Can theoretically scale with data and compute

LLMs (e.g., GPT) are trained in a similar form as IL.

They are trained to predict the next token given a "context" of recent tokens.

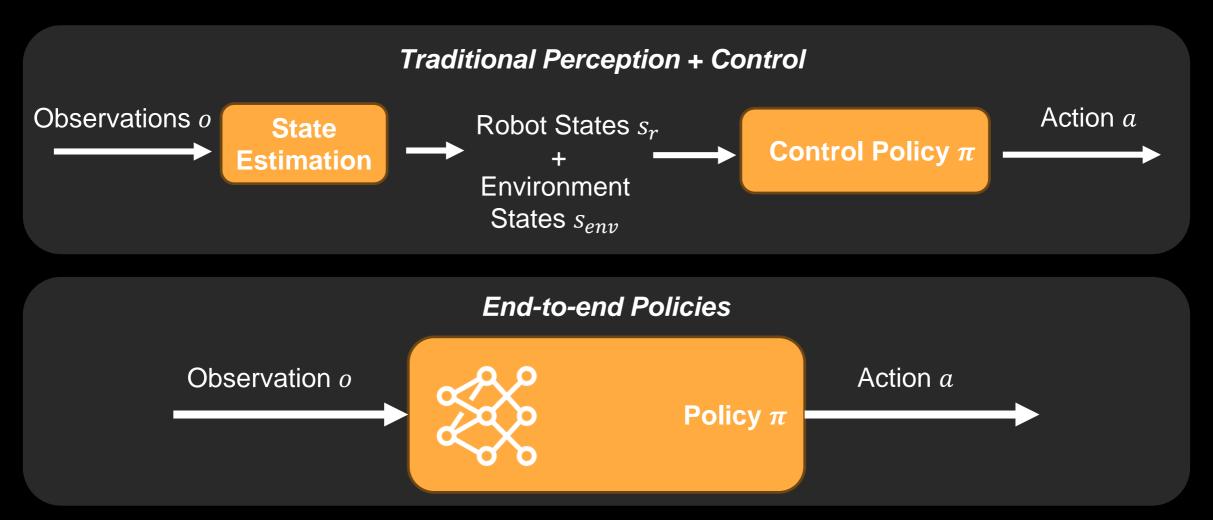
Why is learning actions different than learning next token?





## **Imitation Learning (IL)**

### end-to-end learning





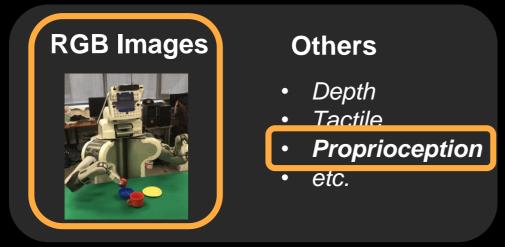


### **Visuomotor Policies**





#### Types of Observations



#### Issues with Observations

Pixel-space is a terrible space to do control

- High dimensional
- Discrete and non-differentiable



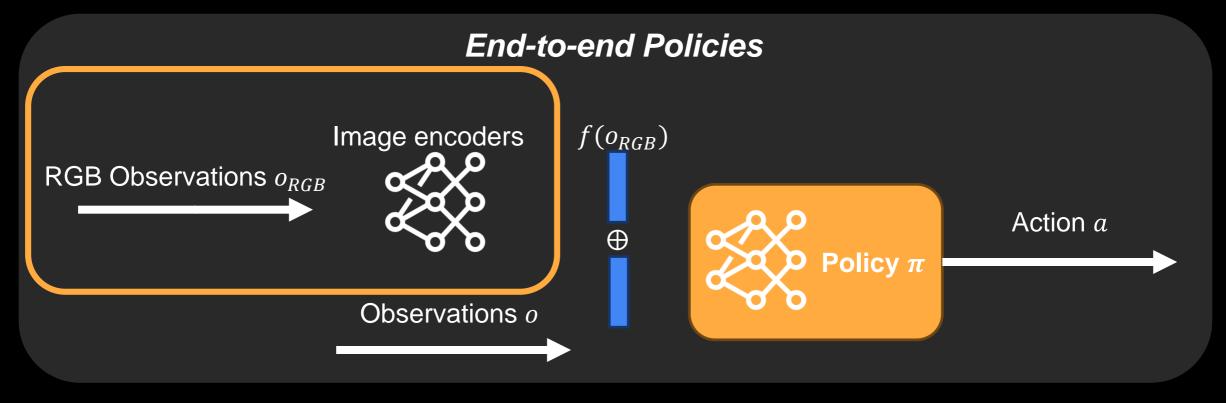
Need latent, meaningful features





## Visuomotor Policies: Encoding Observations





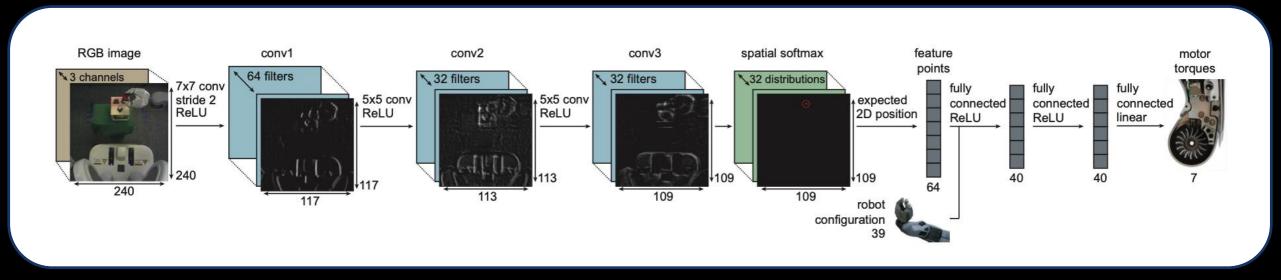




### **Deep Visuomotor Policies**



Sergey Levine\*, Chelsea Finn\*, Trevor Darrell, Pieter Abbeel, "End-to-end training of deep visuomotor policies", *The Journal of Machine Learning Research*, vol. 17, no. 1, pp. 1334--1373, 2016.

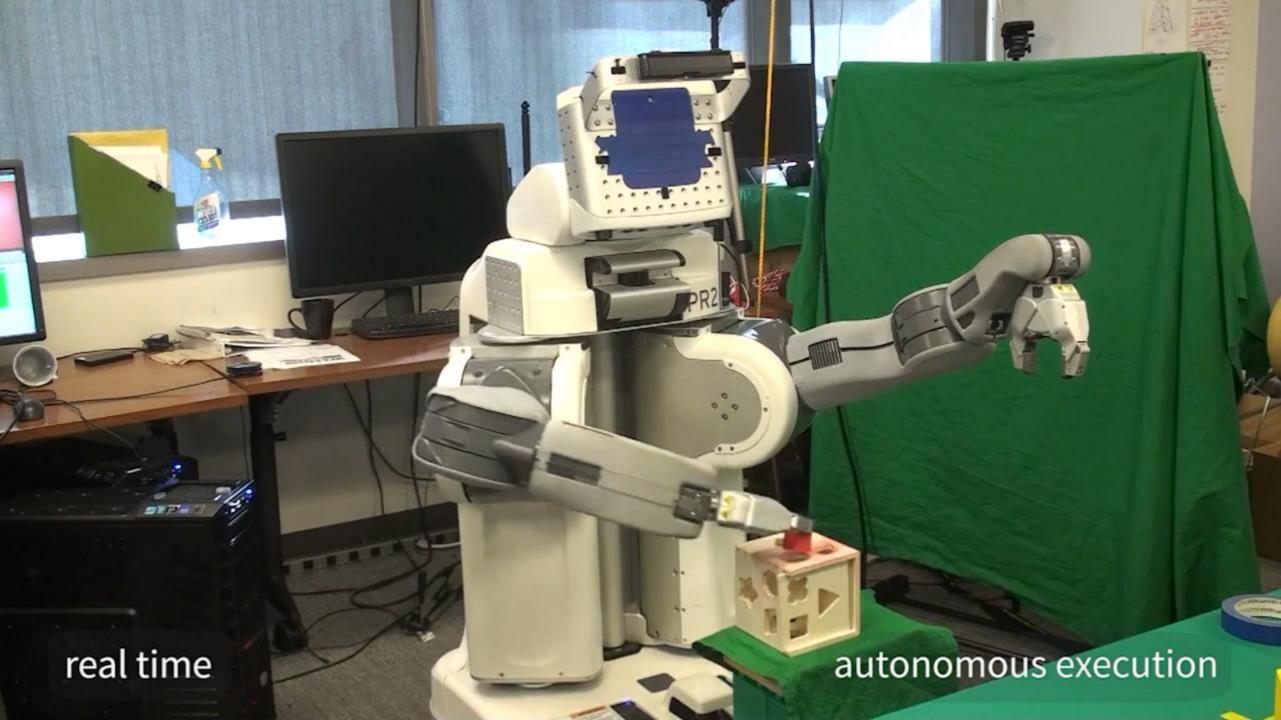


The name "visuomotor" is chosen to emphasize that the policy is trained to predict actions directly from RGB camera images

The action space was directly motor torques. Today, higher level actions are used, and let IK + low-level control transfer to torques



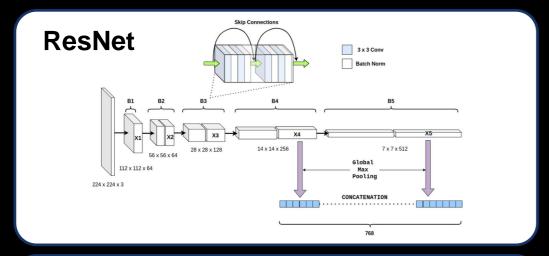


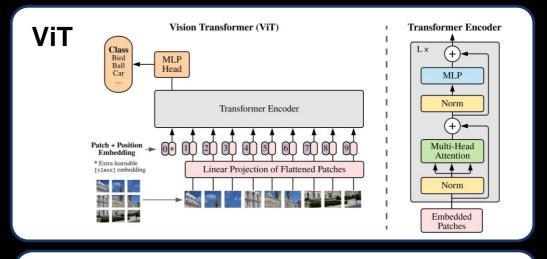


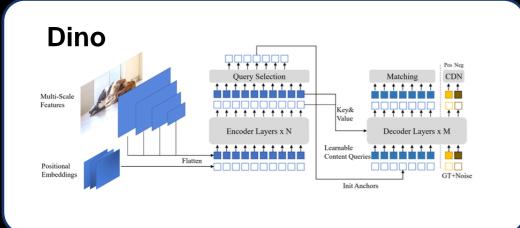
### Visual Encoders Trained on Large Data

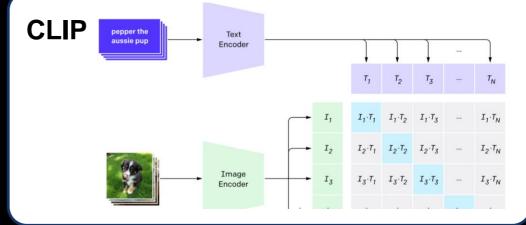


Today, a lot of visual encoders trained on large image datasets









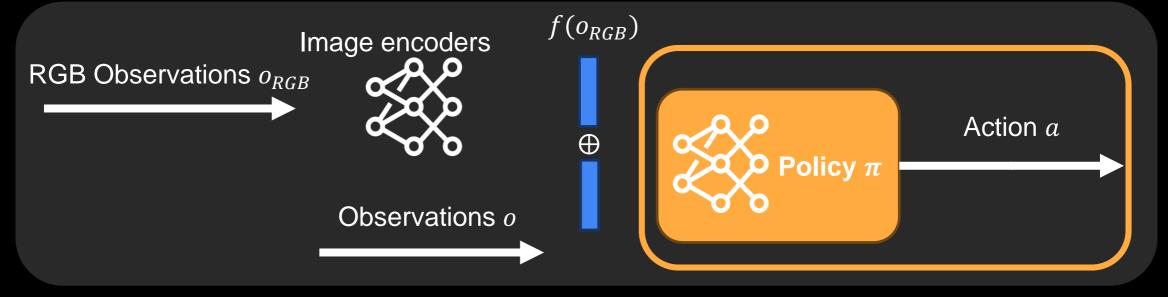


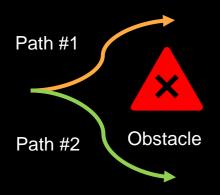


We assume  $f(o_{RGB,t}) = \text{image\_encoder } o_{RGB,t}$ . The policy maps  $\pi$ :  $f(o_{RGB}) + o \rightarrow a$ 

### **Visuomotor Policies: Predicting Actions**







What is the best way to predict actions?

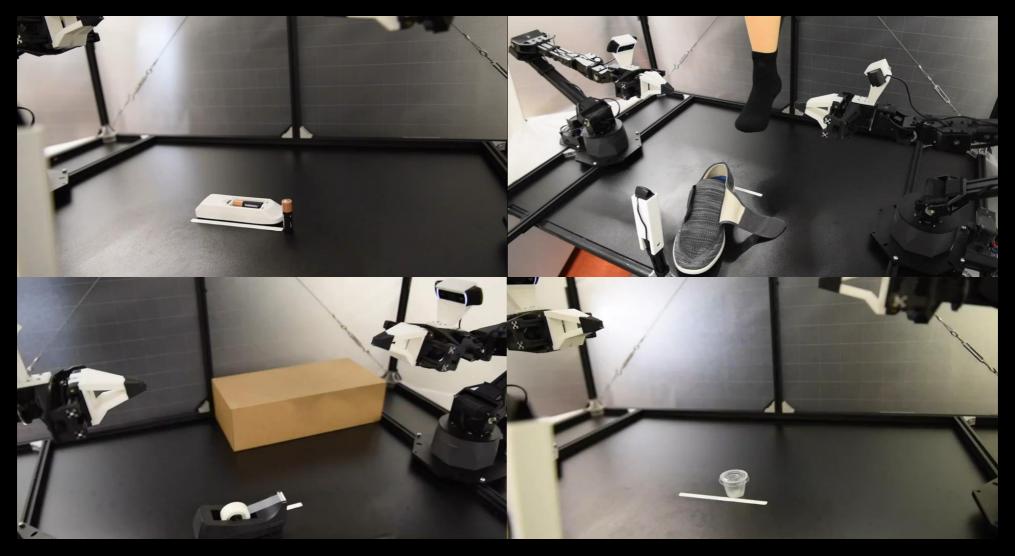
- Multimodality: for the same observation there can be multiple valid actions
- In 2023, *ACT* (Action Chunking Transformers) and *Diffusion Policy* showed convincing capabilities to learn complex dexterous actions





# **ACT (Action Chunking Transformers)**





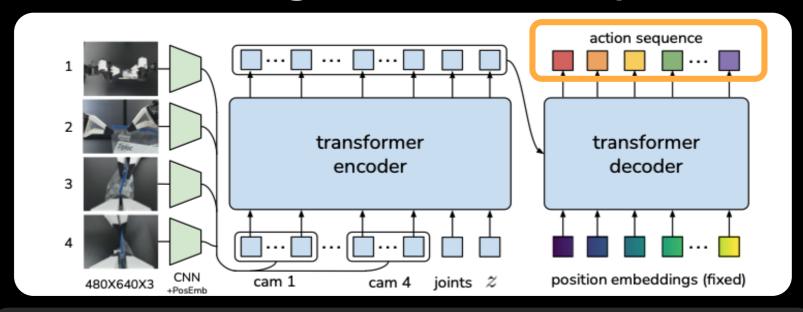




Zhao, T. Z., Kumar, V., Levine, S., Finn, C. (2023). Learning Fine-Grained Bimanual Manipulation with Low-Cost Hardware

# **ACT (Action Chunking Transformers)**





Predict a *chunk* of *k* actions, instead of a single step

$$\pi_{\theta}(a_t|o_t) \rightarrow \pi_{\theta}(a_{t:t+k}|o_t)$$

- Avoid compounding error (wrong predictions quickly leads to out of distribution)
- Shorter horizon control
- Help model non-Markovian behavior (e.g., pauses in the middle of a demonstration)





# **ACT: Temporal Ensemble**



- Naïve implementation of action chunking can be suboptimal
- If new observation is incorporated abruptly every k steps this can result in jerky robot motion



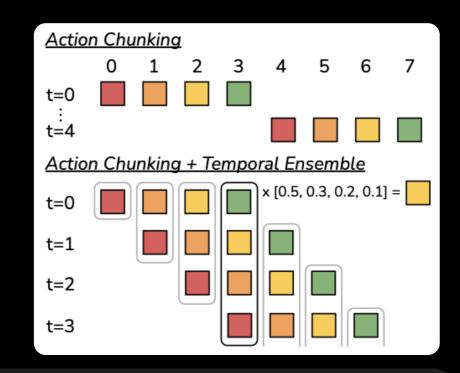




# **ACT**: Temporal Ensemble



- Naïve implementation of action chunking can be suboptimal
- If new observation is incorporated abruptly every k
   steps this can result in jerky robot motion



#### Temporal ensemble

Query the policy at every timestep, aggregate them with a weighted exponential average

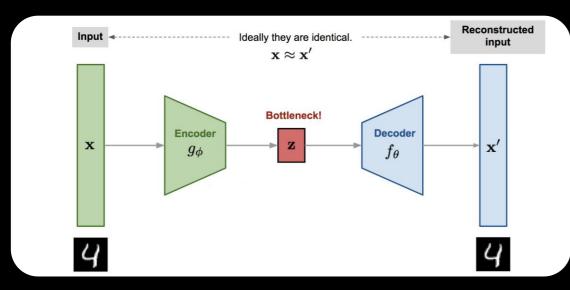
$$w_i = \exp(-m * i)$$

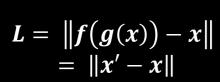


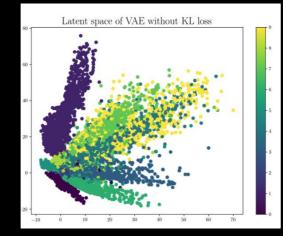


### **ACT: VAEs**

#### **AutoEncoder**



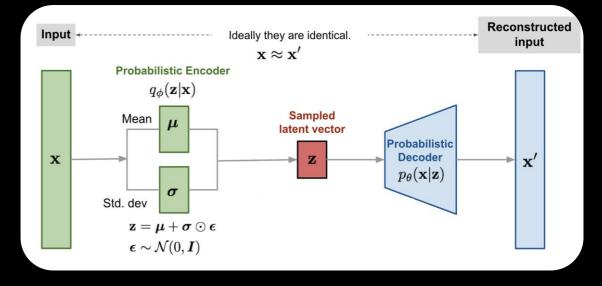


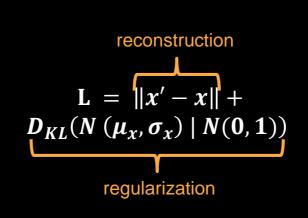


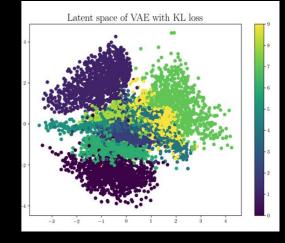




#### **Variational Autoencoder**





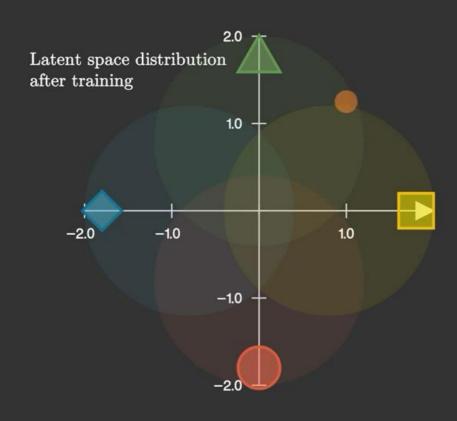


### **ACT: VAEs**



#### Latent space of Variational Autoencoder





Latent space

Latent space is regularized. Vectors sampled from latent space can generate valid data.



Vectors sampled from overlapping distribution generates morphed data.

#### Decoder's output

More on: www.MLinGIFS.aqeel-anwar.com

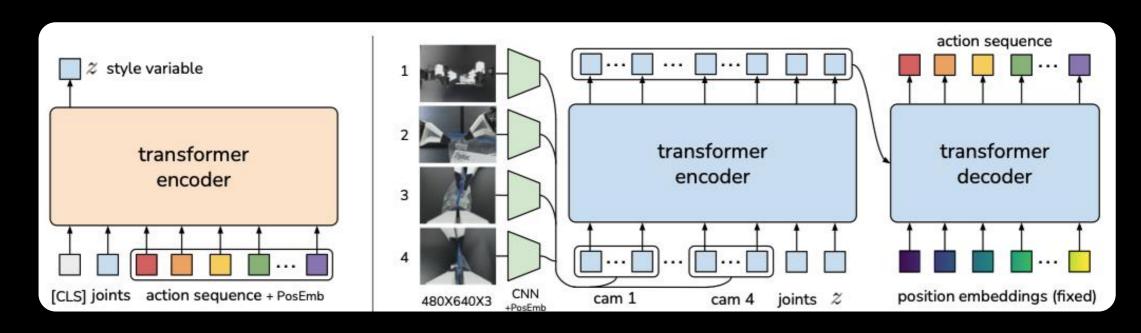




### **ACT: CVAE**



Train the policy as a conditional variational autoencoder (CVAE)



Encoder

$$q_{\phi}(\mathbf{z} | a_{t:t+k}, \overline{o_t})$$

**Conditional Decoder** 

$$\pi_{\theta}(a_{t:t+k-1}|o_t,\mathbf{z})$$

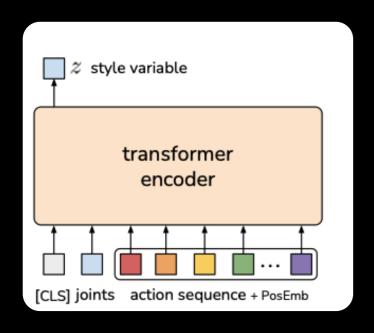








Train the policy as a conditional variational autoencoder



At training time, we encode the action sequence and the proprioception using a transformer

The output is the encoded representation  $\mathbf{z} = q_{\phi}(z \mid a_{t:t+k}, \overline{o_t})$ 

$$\overline{o_t} = o_t - o_{RGB}$$

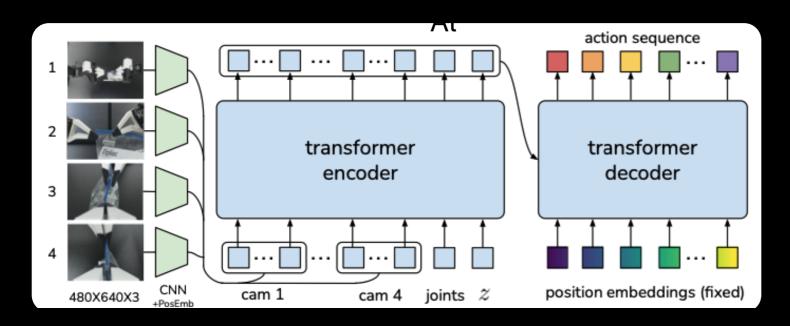




### **ACT: CVAE**



Train the policy as a conditional variational autoencoder



Then, we decode the encoded vector z conditioned on image features and propioception.

$$a_{t_t+k} = \pi_{\theta}(a_{t:t+k-1}|o_t, \mathbf{Z})$$

Training objective is the VAE loss

$$||a_{t:t+k} - \hat{a}_{t:t+k}||^2 + \beta * D_{KL}(\mathcal{N}(\mu_z, \sigma_z), \mathcal{N}(0, 1))$$

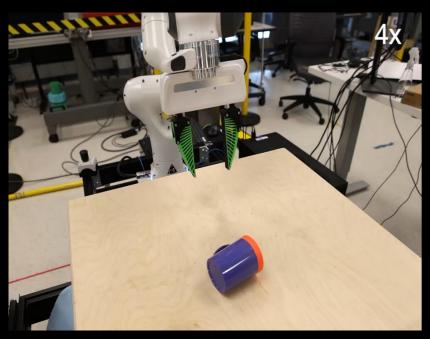
At inference time **z** is set to 0 (mean of the distribution), since we don't have access to future actions

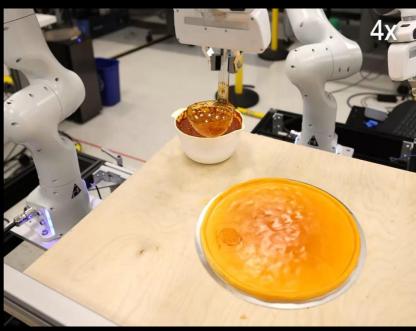


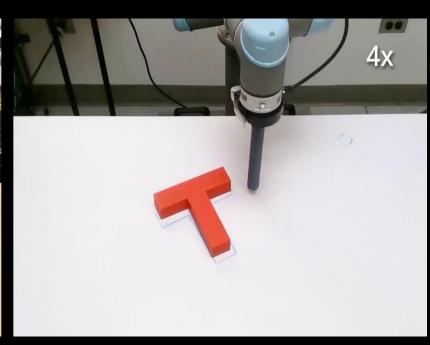


# **Diffusion Policy**









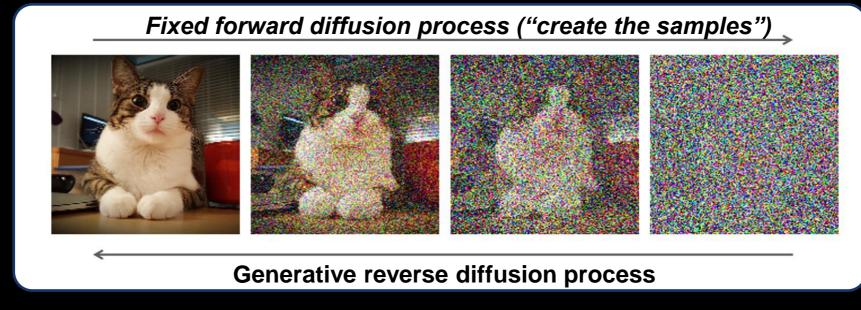
Chi, C. et al. (2023). Diffusion Policy: Visuomotor Policy Learning via Action Diffusion





### **Diffusion Policy – Diffusion Process**





- 1. Sampling  $x_0 \sim \mathfrak{D}$ , noise level  $\sigma \sim [\sigma_{min}, \sigma_{max}]$ , noise  $\epsilon \sim N(0, I)$
- 2. Generating noisy data  $x^{\sigma} = x^{0} + \sigma \epsilon$
- 3. Predicting  $\epsilon$  (direction of noise) from  $x^{\sigma}$  by minimizing squared loss

This amounts to training a  $\theta$ -parametrized neural network  $\epsilon_{\theta}(x, \sigma)$ , by minimizing the loss function  $L(\theta) = \mathbb{E} \left\| \epsilon_{\theta} \left( x^0 + \sigma_t \epsilon, \sigma_t \right) - \epsilon \right\|^2$ 



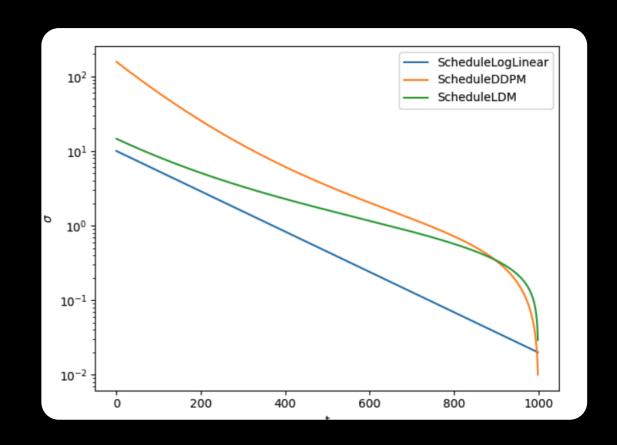


# Diffusion Policy – Diffusion Process



#### How do we add noise?

- In practice,  $\sigma$  is not sampled uniformly in the interval  $[\sigma_{min}, \sigma_{max}]$ , but the interval is discretized into K values called **schedules** and then sampled uniformly between the schedules.
- If we now follow the noise schedule, we can find the denoising formulation
- A well-known scheduler is the ScheduleDDPM (Denoising Diffusion Probabilistics Models)







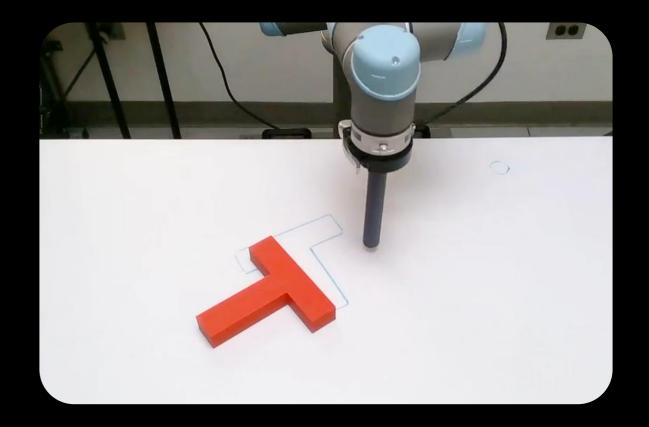
## **Diffusion Policy**



Apply diffusion process to robot action prediction

#### **Advantages**

- Handles multimodal action distribution (many valid actions for a given observation)
- Works in high-dimensional space (e.g., image generation)
- Stable training

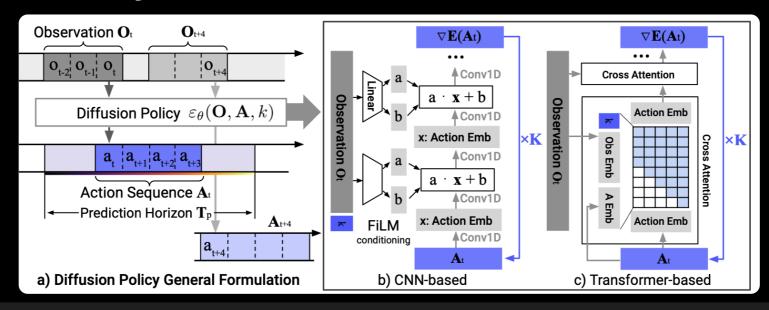






## **Diffusion Policy**





#### **Training**

$$L(\theta) = \left\| \epsilon^k - \epsilon_{\theta}(O_t, A_t^0 + \epsilon^k, k)) \right\|^2$$

 $O_t$ : **history** of observations

 $A_t^0$ : future action sequence

k: noise timestep (scheduler)

t: action timestep

#### **Denoising Process**

We use a DDPM to approximate the conditional distribution  $p(A_t | O_t)$ 

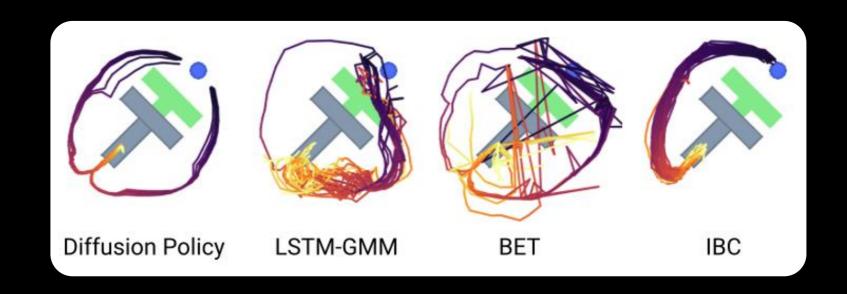
$$\mathbf{A_t^{k-1}} = \alpha \left( \mathbf{A_t^k} - \gamma \varepsilon_{\theta} (\mathbf{O_t}, \mathbf{A_t^k}, k) + \mathcal{N}(0, \sigma^{2I}) \right)$$





### **Diffusion Policy - Multimodality**





#### Diffusion Policy naturally models multimodal action distributions:

• Each rollout commits to a coherent action mode, but different rollouts represent different valid strategies - capturing true multimodality.



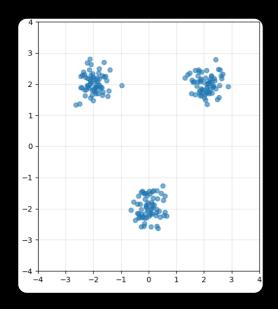


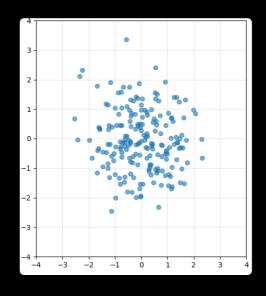
## Side quest: Flow Matching



#### Diffusion

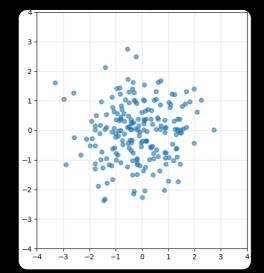
Real data distribution





Diffusion Models gradually add noise to data until it becomes pure noise, then learn to reverse this process

Flow Matching



Flow matching creates a continuous path (or flow) between noise and data distribution





## Side quest: Flow Matching



```
# DDPM: learn to predict noise
         for each training step:
             x0 = sample_data()
             t = random_timestep()
             # Add noise
             eps = random_noise()
Noise scheduler xt = add_noise(x0, eps, t)
             # Predict the noise
             eps_pred = model(xt, t)
             # Trai
                                        noise
                    MSE(eps_pred, eps)
             loss
             update(model, loss)
```

```
# Flow Matching: learn velocity from noise → data
for each training step:
   x0 = sample data()
   z = random noise()
      = random_time_between_0_and_1()
   # Point along straight line from noise to data
   xt = (1 - t) * z + t * x0
   # Target velocity field
   v_{target} = x0 - z
   # Predict velocity
   v pred = model(xt, t)
   # Train to match the velocity
          MSE(v_pred, v_target)
   loss =
   update(model, loss)
```





### **Key Takeaways**



- Imitation Learning turns control into supervised learning
- Pixels become useful through feature encoders
- Demonstrations are noisy & multimodal
  - → generative models (CVAE in ACT, diffusion in DP) capture variability and improve precision in challenging manipulation tasks.

Next lecture: From single-task to multi-task? What happens if we scale the model up? **VLA models** 





### Acknowledgements and useful resources



- MIT 6.8210 Underactuated Robotics, chapter 21 <a href="https://underactuated.mit.edu/imitation.html">https://underactuated.mit.edu/imitation.html</a>
- Diffusion models :
  - (easy): <a href="https://chenyang.co/diffusion.html">https://chenyang.co/diffusion.html</a>
  - (more complex) <a href="https://lilianweng.github.io/posts/2021-07-11-diffusion-models/">https://lilianweng.github.io/posts/2021-07-11-diffusion-models/</a>
- Flow matching vs Diffusion <a href="https://harshm121.medium.com/flow-matching-vs-diffusion-79578a16c510">https://harshm121.medium.com/flow-matching-vs-diffusion-79578a16c510</a>
- Diffusion and Flow models lecture <a href="https://arxiv.org/pdf/2506.02070">https://arxiv.org/pdf/2506.02070</a>
- Levine, S., Finn, C., Darrell, T., & Abbeel, P. (2016). End-to-End Training of Deep Visuomotor Policies. JMLR, 17(1), 1334-1373.
- Chi, C. et al. (2023). Diffusion Policy: Visuomotor Policy Learning via Action Diffusion. arXiv:2303.04137.
- Zhao, T. Z., Kumar, V., Levine, S., Finn, C. (2023). *Learning Fine-Grained Bimanual Manipulation with Low-Cost Hardware* (introduces ACT). arXiv:2304.13705.



