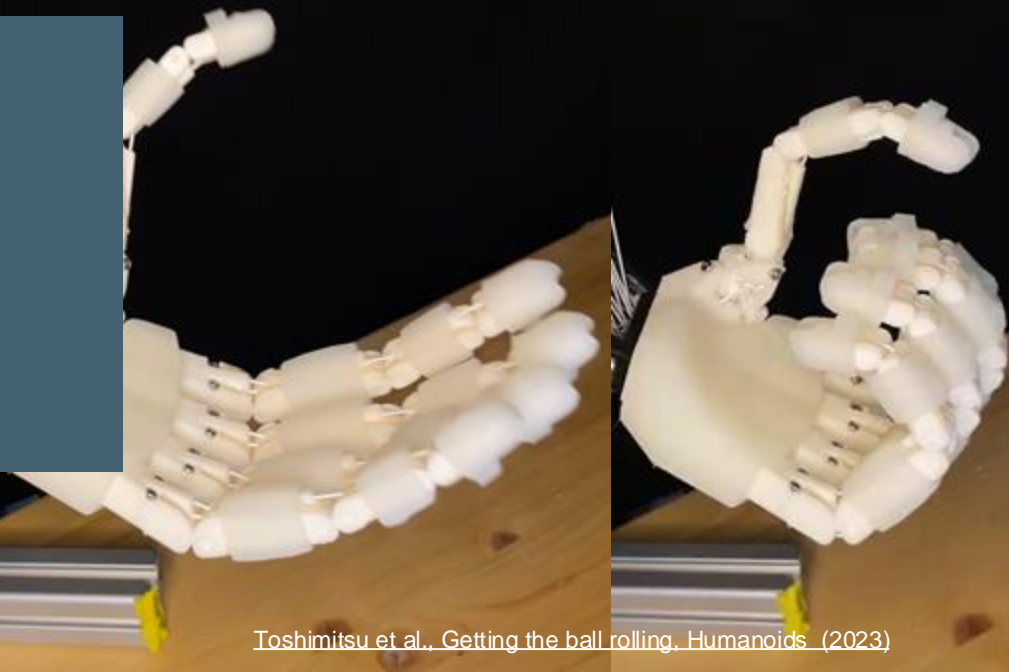




Control Challenges for Dexterous Manipulation

Robert Katzschmann

Soft Robotics Lab



Toshimitsu et al., Getting the ball rolling. Humanoids (2023)

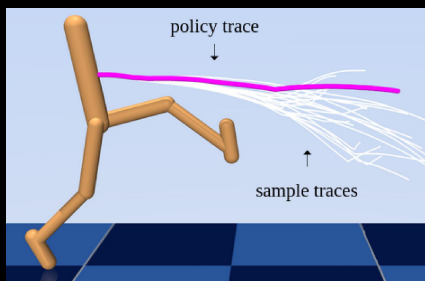


Plan for Today

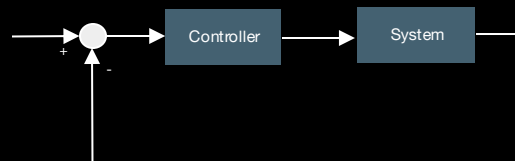
1. Sensing



2b. Model Predictive Control



2a. Feedback Control



3. Challenges

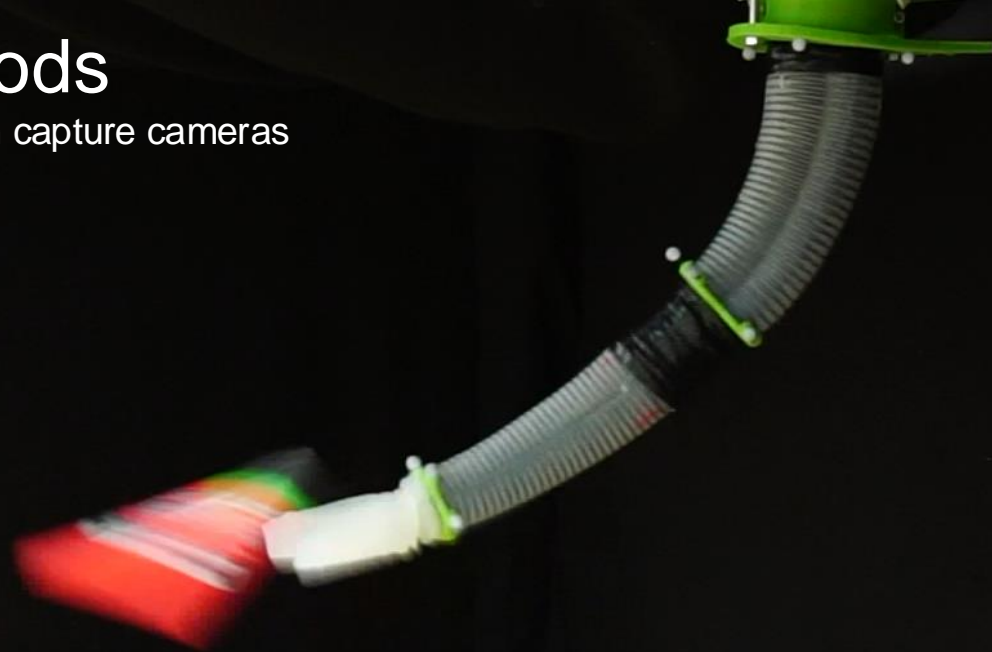




Part 1: Sensing

Direct methods

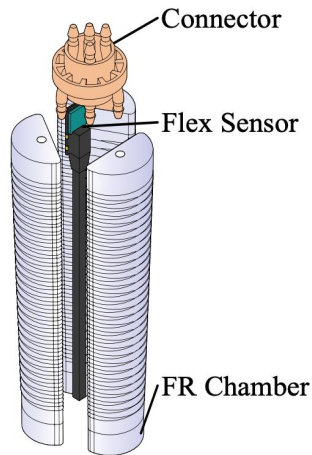
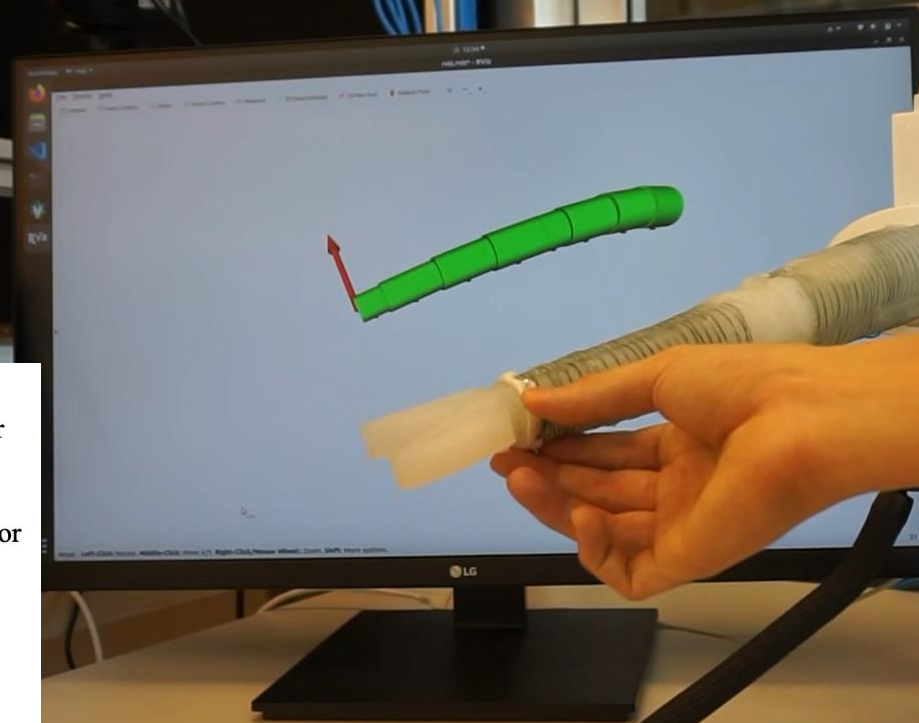
such as external motion capture cameras



Fischer, O., Toshimitsu, Y., Kazemipour, A., & Katzschmann, R. K. (2023). Dynamic Task Space Control Enables Soft Manipulators to Perform Real-World Tasks. *Advanced Intelligent Systems*, 5(1), 2200024.

Indirect methods

such as built-in flex sensors

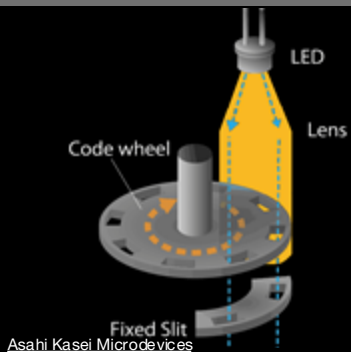


Toshimitsu, Y., Wong, K. W., Buchner, T., & Katzschmann, R. (2021, September). Sopra: Fabrication & dynamical modeling of a scalable soft continuum robotic arm with integrated proprioceptive sensing. In *2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)* (pp. 653-660). IEEE.



Sensor options

Rotary Encoders

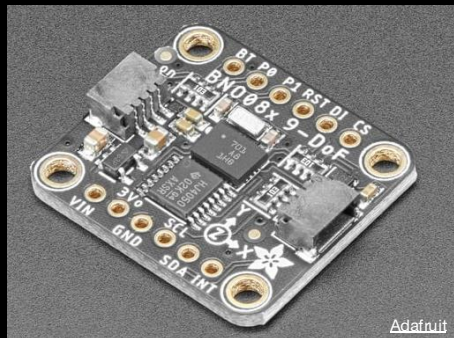


Flex Sensors

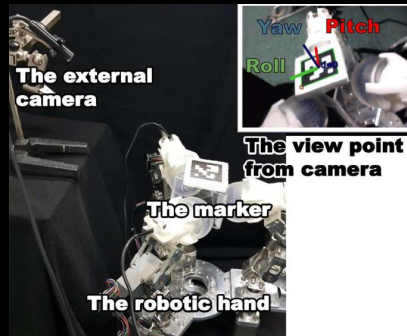


AdaFruit

Inertial Measurement Unit

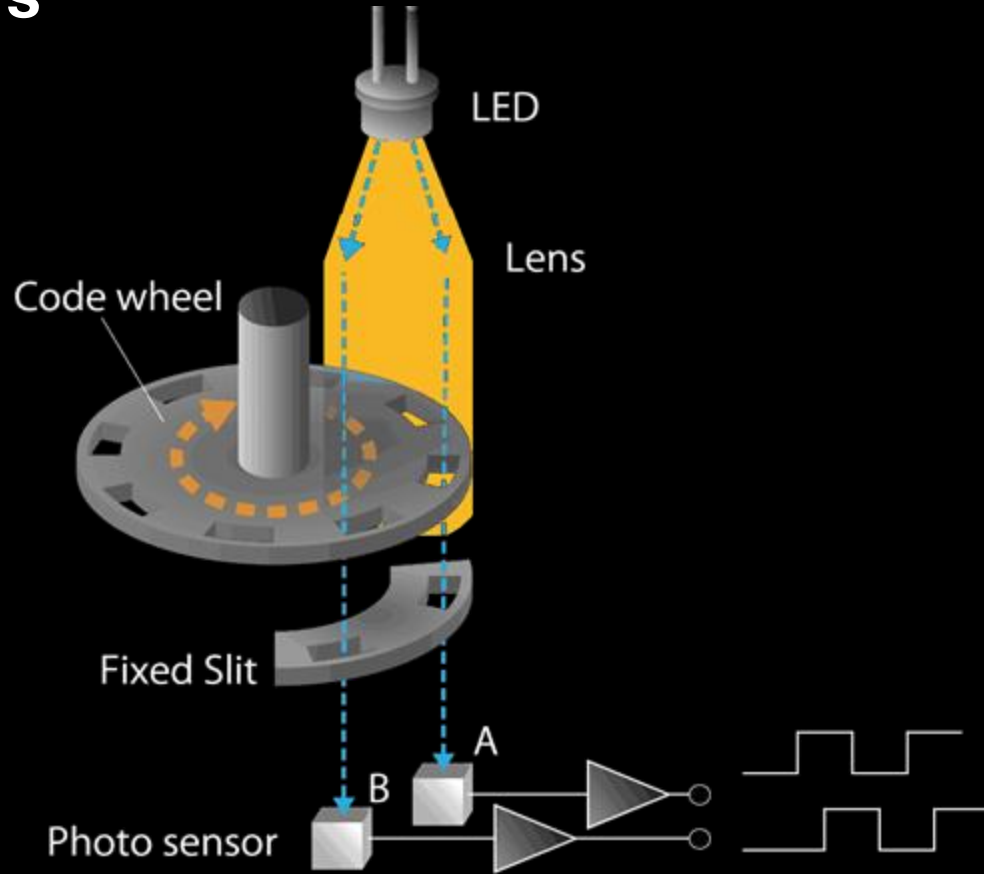


Camera



Choi_Tahara_Robomech_Journal(2020)

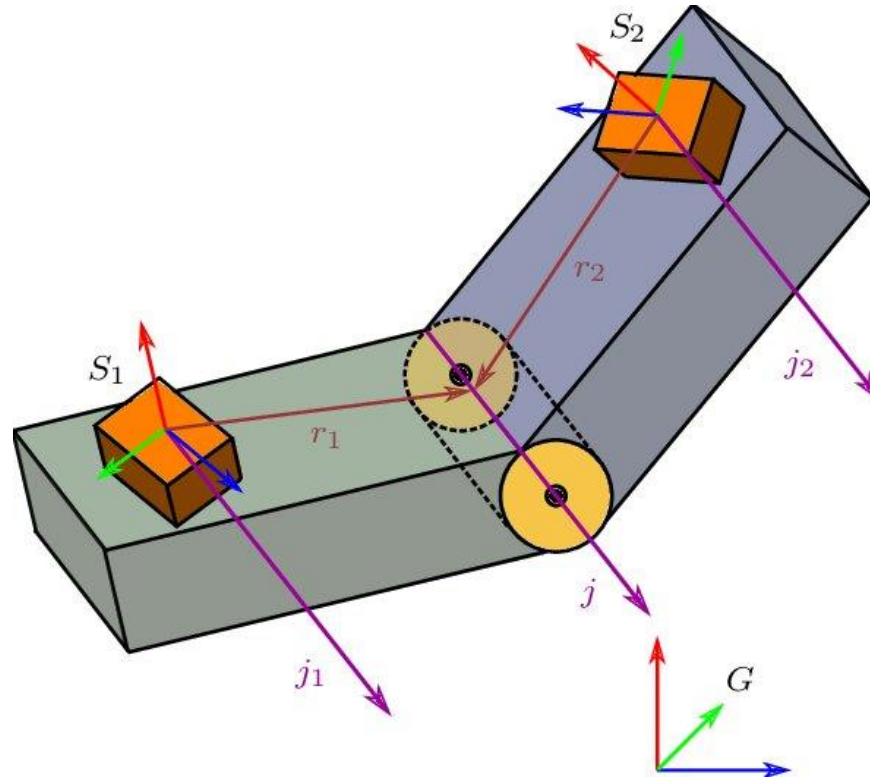
Rotary Encoders

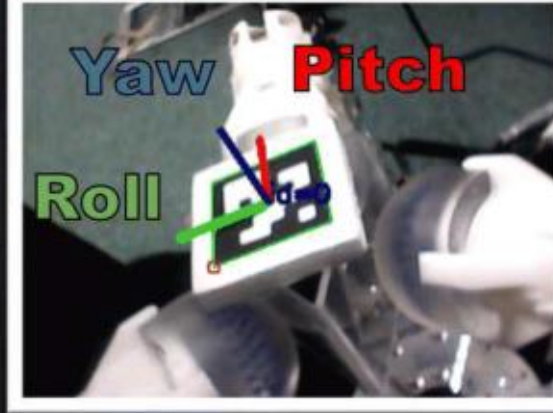


Flex Sensors



Inertial Measurement Unit





The view point from camera

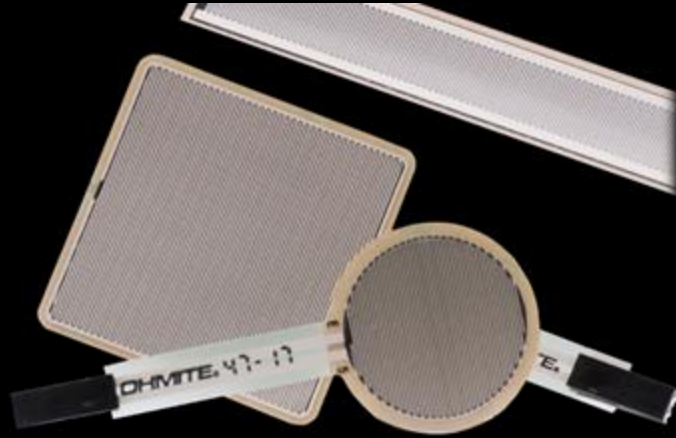
The marker

The robotic hand

Sensing the touch:

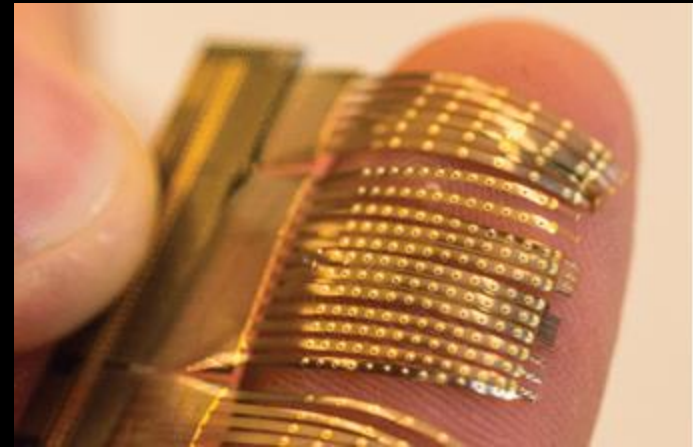


Force Sensing Resistors



Ohmite

Artificial Skin



Weichart et al. *Tactile Sensing With Scalable Capacitive Sensor Arrays on Flexible Substrates* (2021)

Kalman Filter – The Intuition



Optimal state estimate

\hat{x}_k

Predicted state estimate

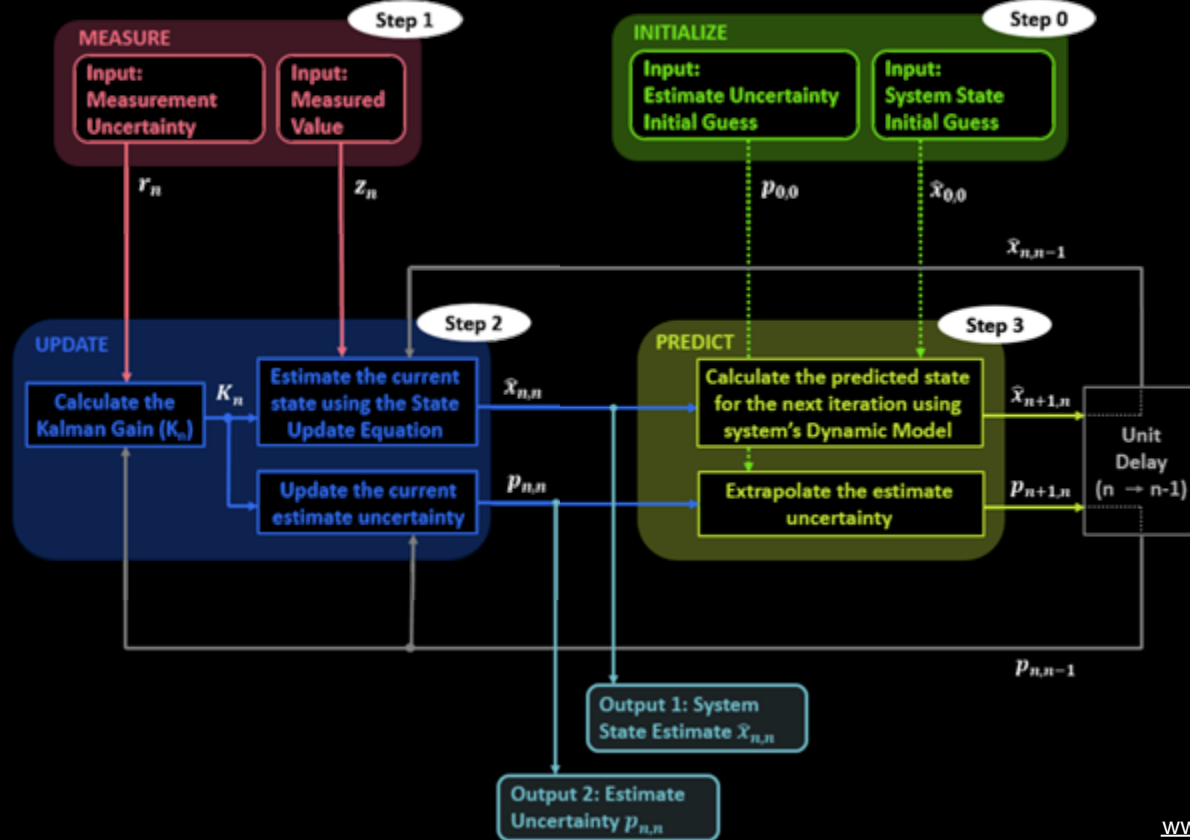
Measurement

\hat{x}_k

y_k



Kalman Filter

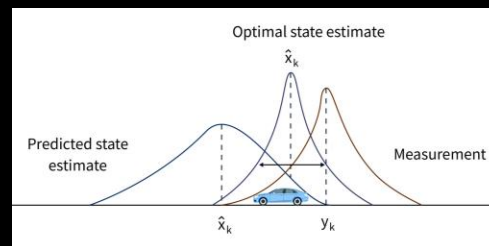


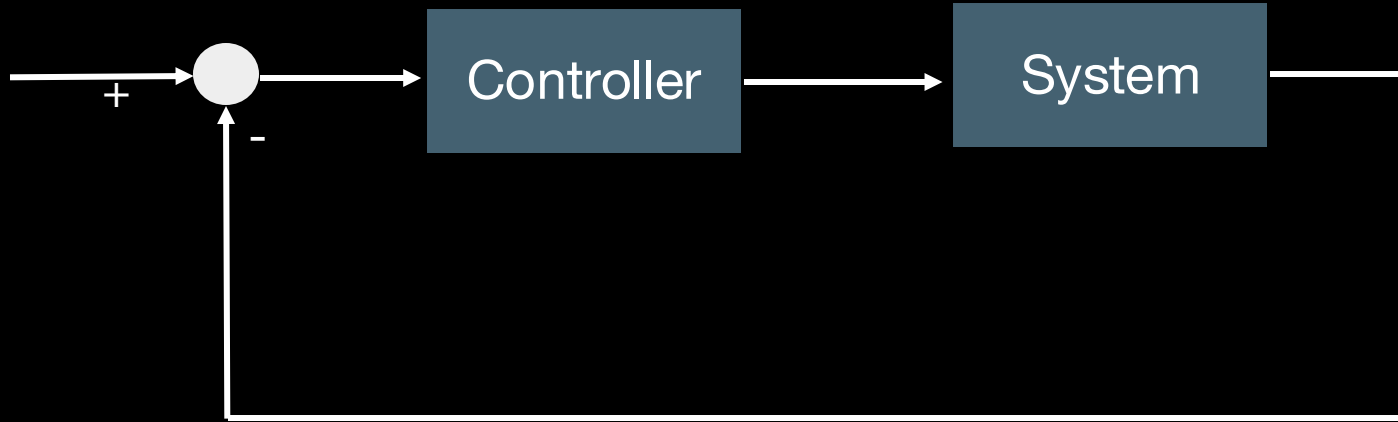
www.kalmanfilter.net



Sensing Summary

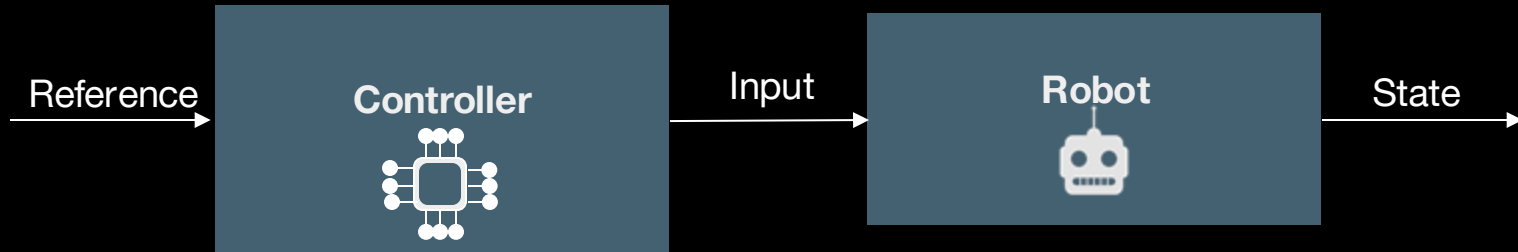
- **Pose** estimation
 - Measure absolute pose
 - Measuring relative pose
- **Force** estimation
 - Force Sensing Resistors
 - Artificial Skin
- **Kalman Filter**



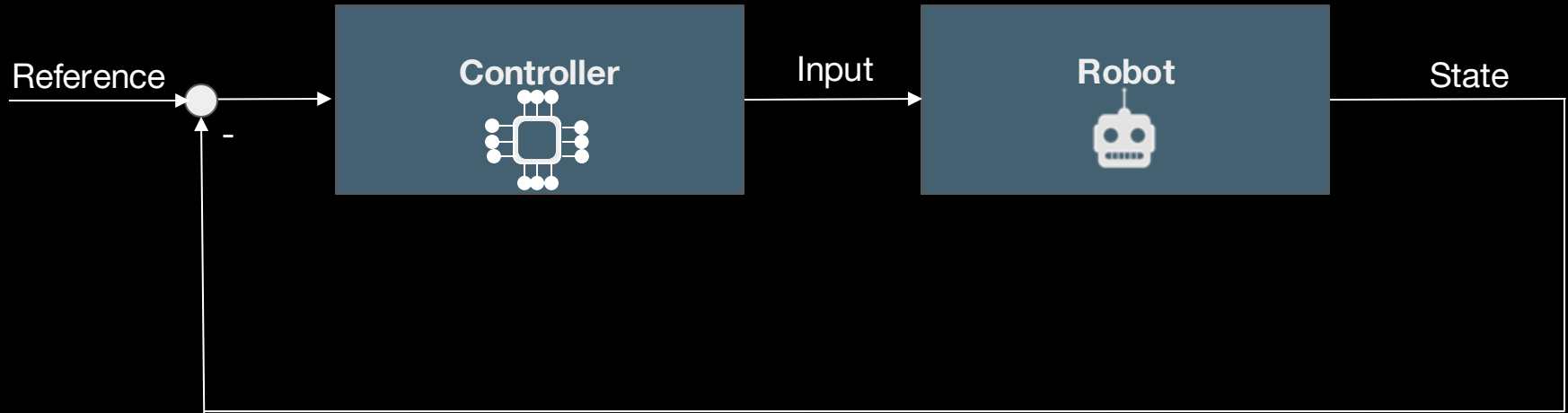


Part 2a: Feedback Control

Simplest controller possible: Open loop



Closed Loop Controller





Inverse Kinematics

- From greek *kinema* = motion
- In the past units we learnt that:

$$J(q)\dot{q} = \chi_e = \begin{bmatrix} \dot{p}_e \\ w_e \end{bmatrix}$$

- If we invert it we obtain:

$$\dot{q} = J^+ \chi_e \text{ with } J^+ = J^T (J J^T)^{-1}$$

- And in a differential form:

$$\Delta \chi_e = J^+ \Delta q$$

Algorithm 1 Numerical Inverse Kinematics

```

1:  $q \leftarrow q^0$  ▷ Start configuration
2: while  $\|\chi_e^* - \chi_e(q)\| > tol$  do ▷ While the solution is not reached
3:    $J_{eA} \leftarrow J_{eA}(q) = \frac{\partial \chi_e}{\partial q}(q)$  ▷ Evaluate Jacobian for  $q$ 
4:    $J_{eA}^+ \leftarrow (J_{eA})^+$  ▷ Calculate the pseudo inverse
5:    $\Delta \chi_e \leftarrow \chi_e^* - \chi_e(q)$  ▷ Find the end-effector configuration error vector
6:    $q \leftarrow q + J_{eA}^+ \Delta \chi_e$  ▷ Update the generalized coordinates
7: end while

```

A possible inverse kinematics algorithm

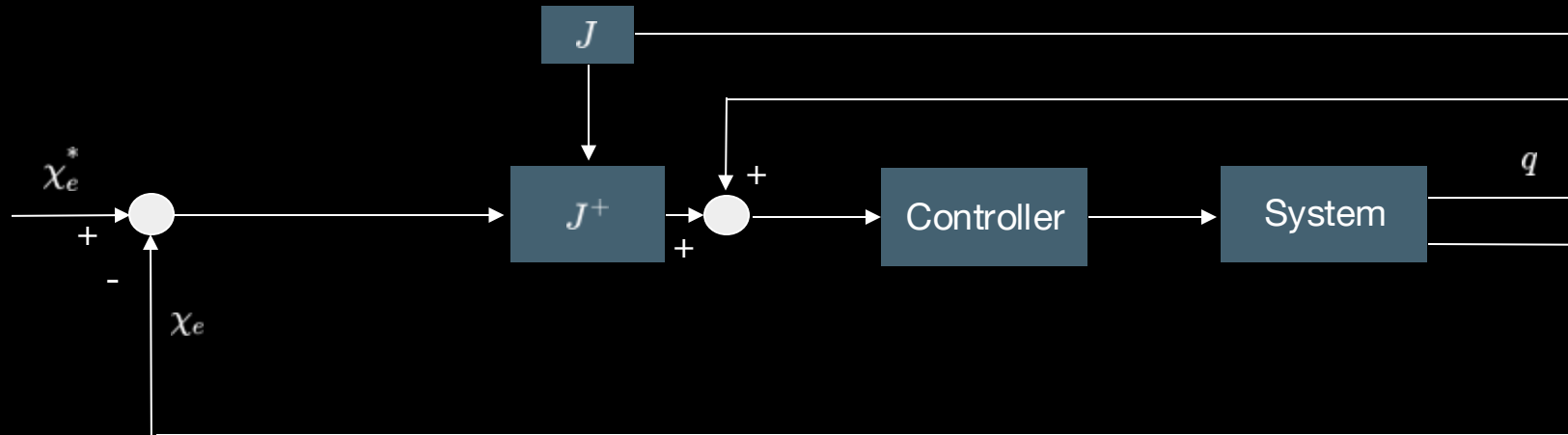
Robot Dynamics Class @ ETH Zurich

To overcome stability issues, the update can be scaled by a factor k

$$q \leftarrow q + k J_{eA}^+ \Delta \chi_e \text{ with } k \in (0, 1)$$

-> slower convergence

Inverse Kinematics Control





Trajectory Control

We can use a closed loop controller, but we need to add a component for the desired velocities

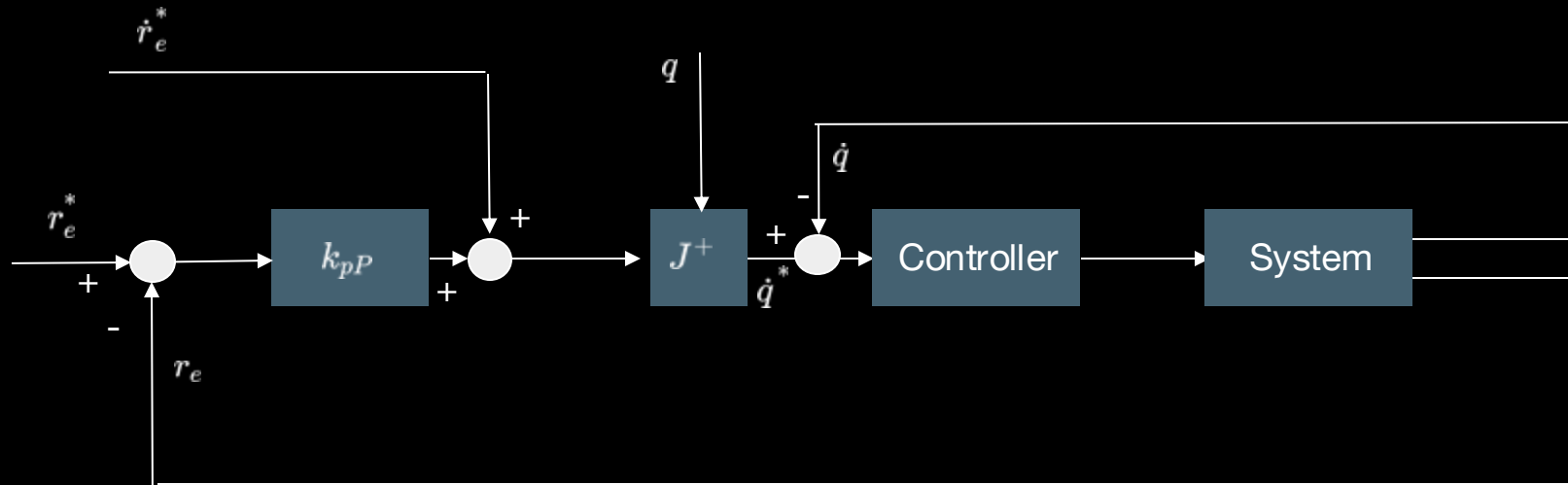
We define $\Delta r_e^t = r_e^*(t) - r_e(q^t)$

And the desired joint velocity $\dot{q}^* = J_{e0P}^+(q^t) \cdot (\dot{r}_e^*(t) + k_{pP}\Delta r_e^t)$

If we have a desired rotation rate we write $\dot{q}^* = J_{e0R}^+(q^t) \cdot (\omega_e^*(t) + k_{pR}\Delta\phi)$

Where ϕ are the angles used to represent the orientation of the end effector.

Trajectory Control





Dynamic control

The dynamic model is

$$M(q)\ddot{q} + b(q, \dot{q}) + g(q) = \tau + J_c(q)^T F_c$$

With:

$M(q)$: Generalized mass matrix

q, \dot{q}, \ddot{q} : Generalized position, velocity and acceleration vector

$b(q, \dot{q})$: Coriolis and centrifugal terms

$g(q)$: Gravitational terms

τ : External generalized forces

F_c : External Cartesian forces

$J_c(q)$: Geometric Jacobian corresponding to the external forces



Dynamic control

The dynamic model is

$$M(q)\ddot{q} + b(q, \dot{q}) + g(q) = \tau + J_c(q)^T F_c$$

If we know the desired generalized accelerations, velocities and poses we can write

$$\ddot{q}^* = k_p(q^* - q) + k_d(\dot{q}^* - \dot{q})$$

Thus the joint torques will be

$$\tau^* = M(q)\ddot{q}^* + b(q, \dot{q}) + g(q)$$



Task-space control

Remember that $J(q)\dot{q} = \chi_e = \begin{bmatrix} \dot{p}_e \\ w_e \end{bmatrix}$

If you derive that with respect to time: $\dot{\chi}_e = J(q)\ddot{q} + \dot{J}(q)\dot{q}$

And if we solve the dynamics equation for the joint acceleration and substitute in the equation above we get: $\dot{\chi}_e = JM^{-1}(\tau - b - g) + \dot{J}\dot{q}$

Finally, remembering that $\tau = J_e^T F_e$

We can write $\Lambda_e \dot{\chi}_e + \mu + p = F_e$

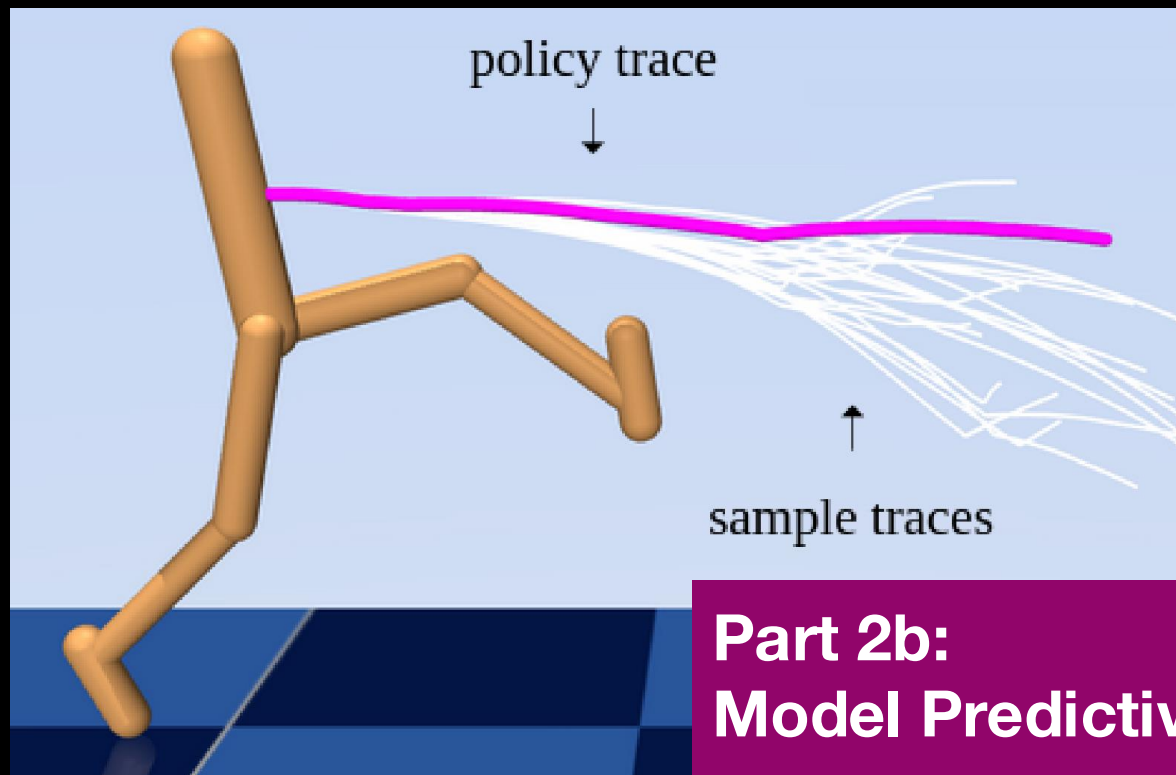
$$\begin{aligned}\Lambda_e &= (J_e M^{-1} J_e^T)^{-1} \\ \mu &= \Lambda_e J_e M^{-1} b - \Lambda_e \dot{J}_e \dot{q} \\ p &= \Lambda_e J_e M^{-1} g\end{aligned}$$



Task-space control

Defining the dynamics uniquely depending on the state of the end effector allows us to design a control loop

$$\dot{\chi}_e^* = \begin{pmatrix} r_e^* - r_e \\ \Delta\phi_e \end{pmatrix} + k_d(\chi_e^* - \chi_e)$$



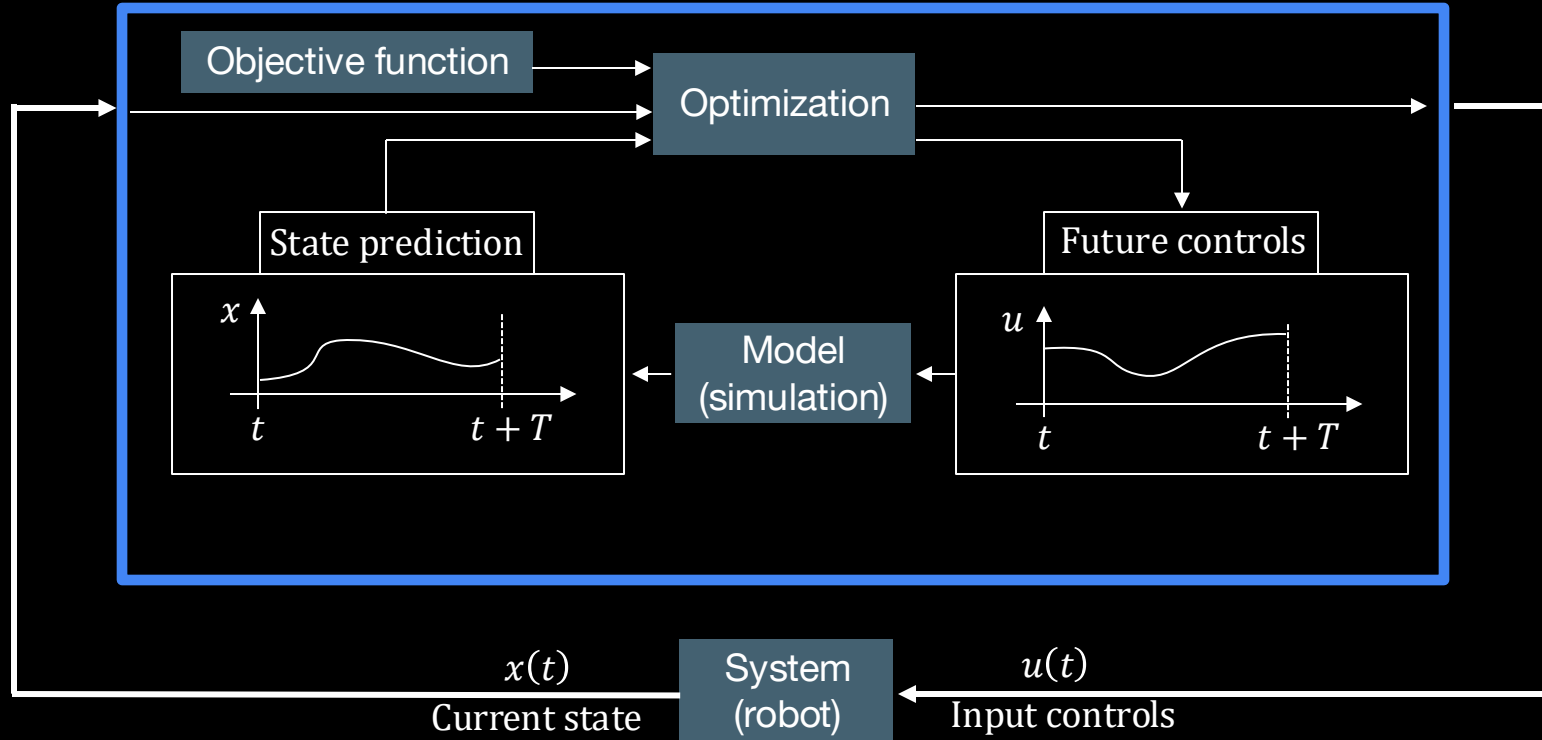
**Part 2b:
Model Predictive Control**

[Mujoco PC](#)

Model predictive control



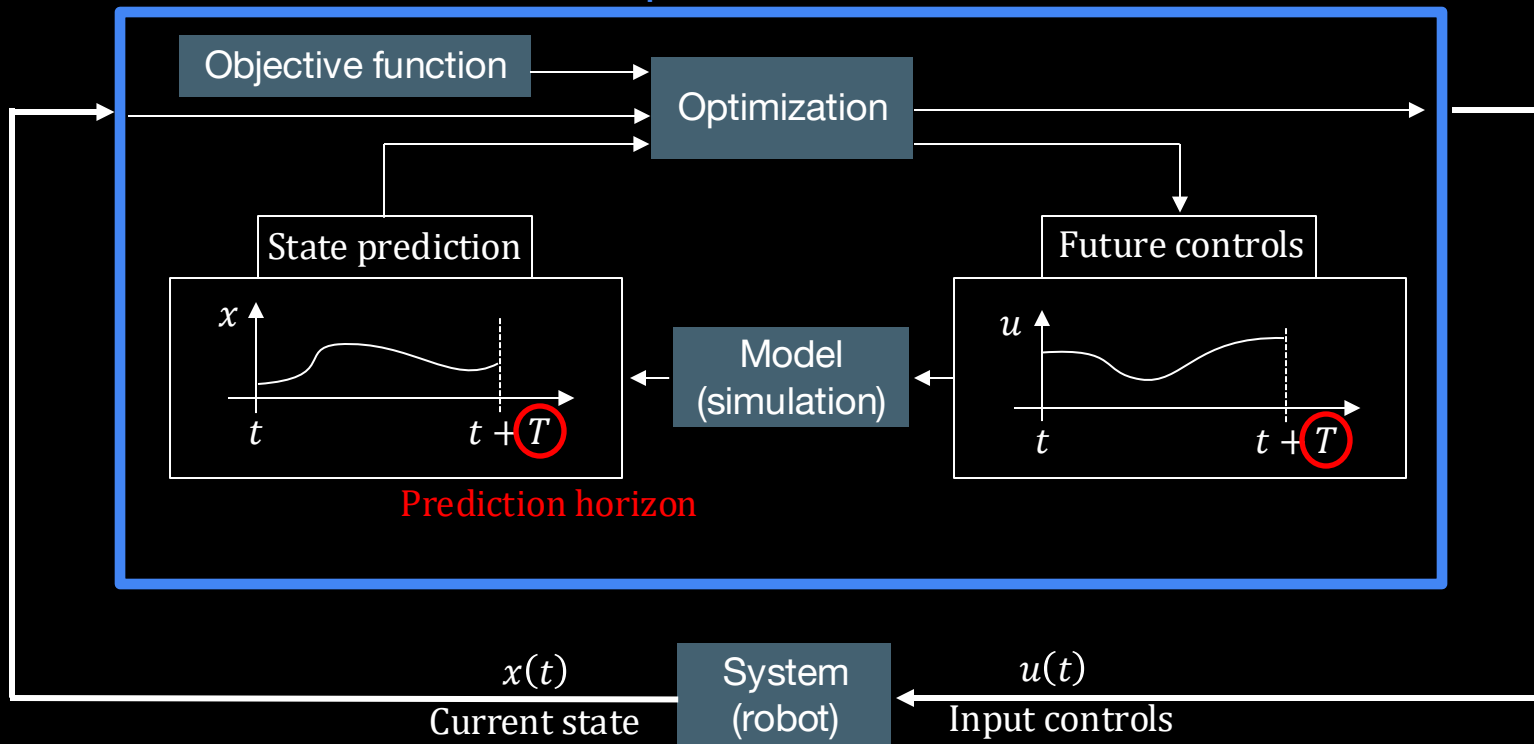
Model predictive controller





Model predictive control

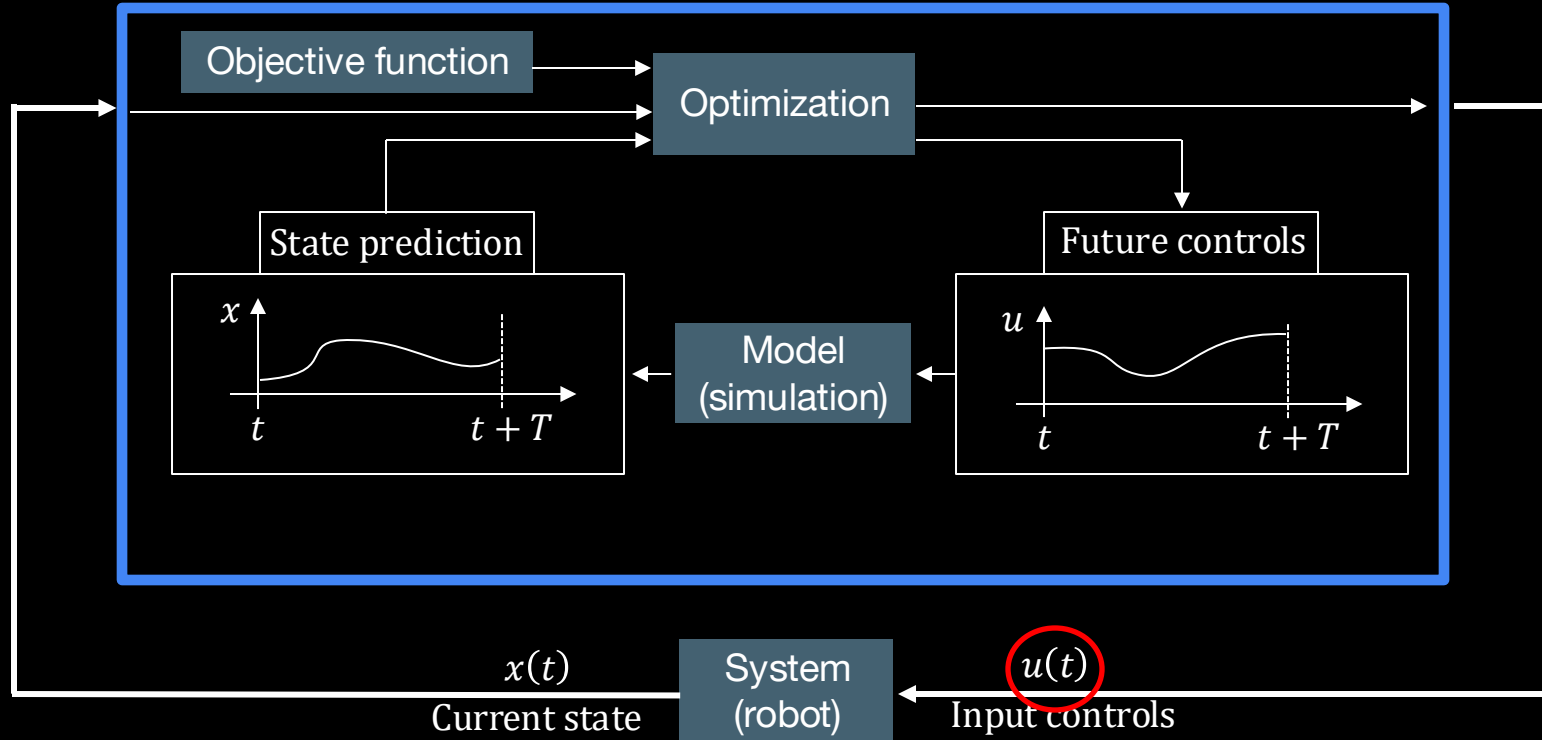
Model predictive controller



Model predictive control



Model predictive controller

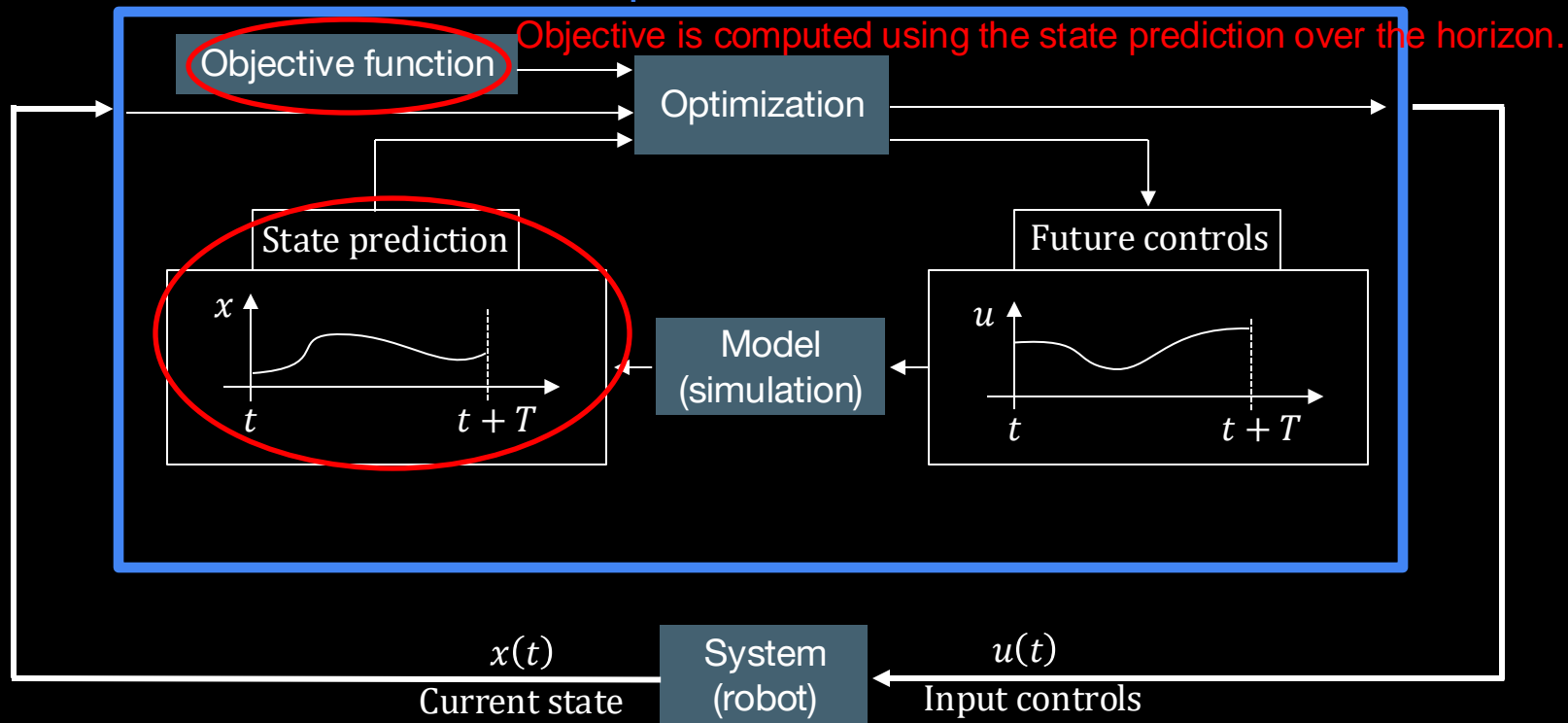


Execute only the “next step”,
not the whole prediction horizon.

Model predictive control



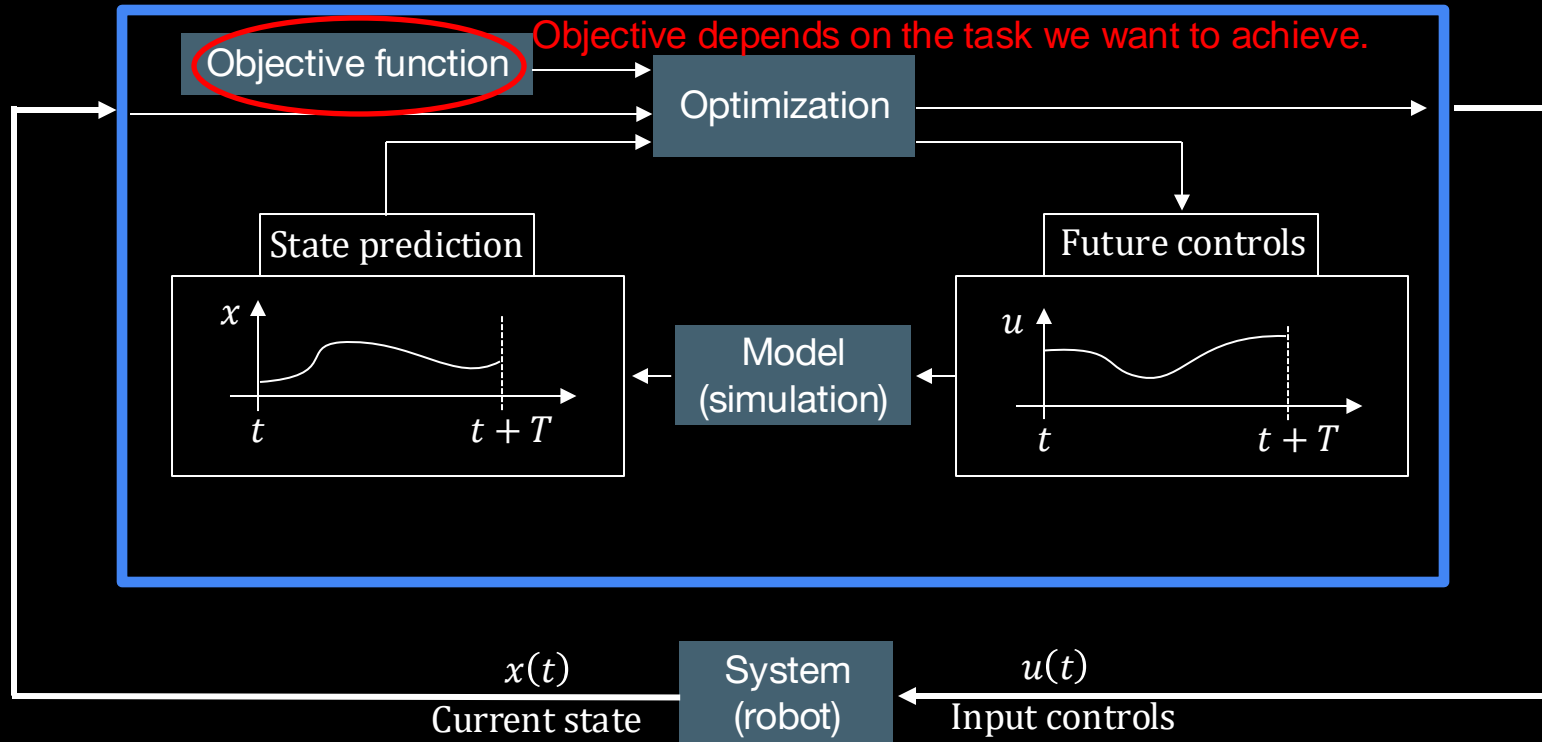
Model predictive controller



Model predictive control



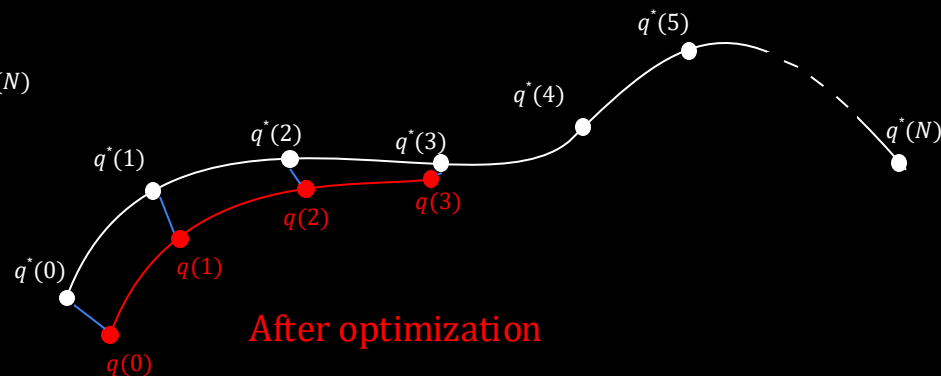
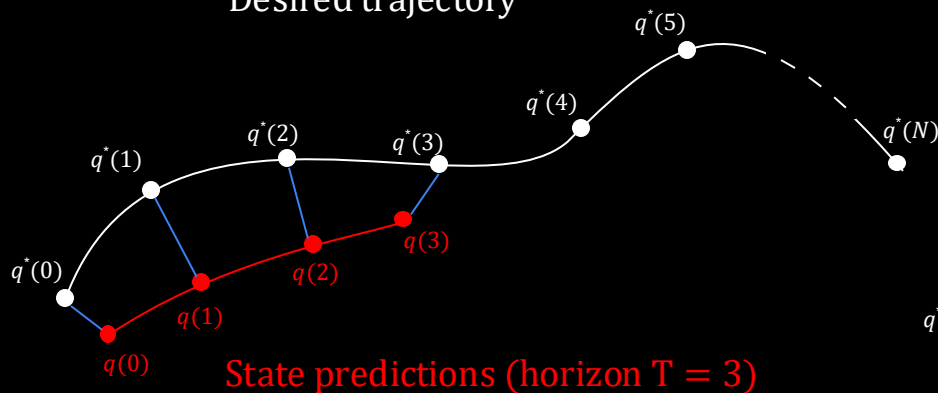
Model predictive controller





Trajectory following with MPC

Desired trajectory



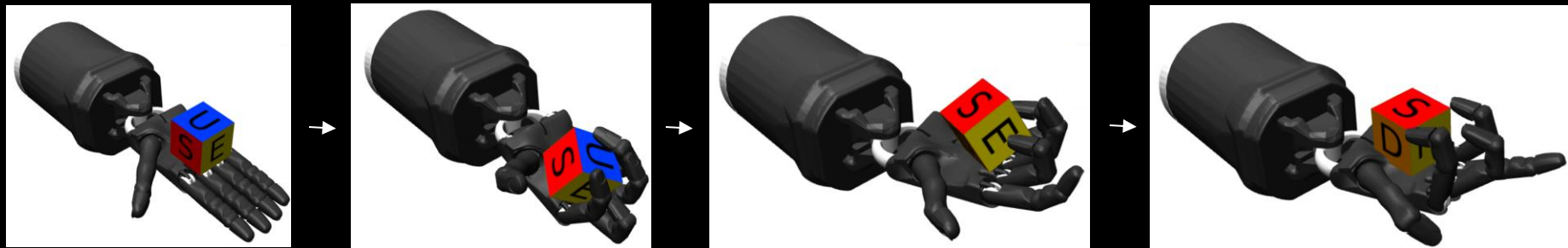
$$\text{Objective } J = \sum_{t=0}^T c(t)$$

where each step cost $c(t) = \|q^*(t) - q(t)\|_2$



Cube reorientation with MPC

Goal orientation:

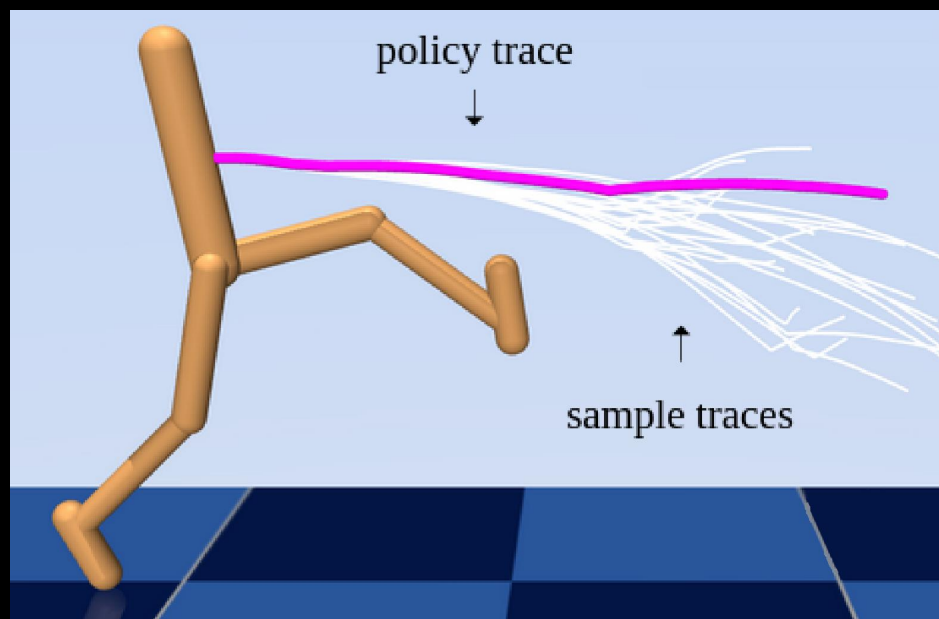


System state $x(t)$ includes robot state $q(t)$, but also the object state.

$$\text{Objective } J = \sum_{t=0}^T c(t)$$

where $c(t) = \|\text{cube orientation}(t) - \text{goal orientation}\|_2 + \|\text{cube position}(t) - \text{palm center}\|_2$

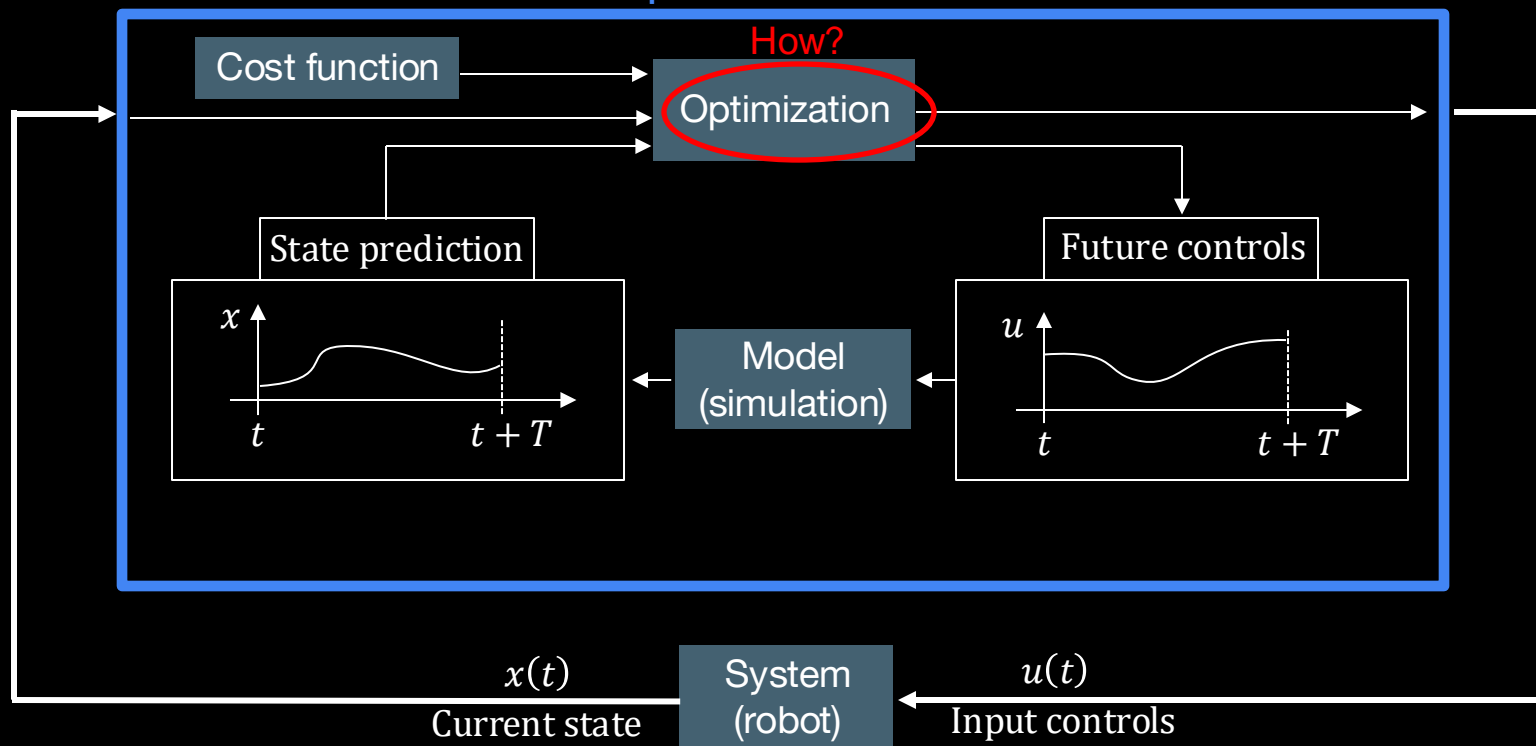
Mujoco Predictive Control (MJPC) Demo



Model predictive control



Model predictive controller





Trajectory optimization

Given current state $x(0)$

$$\min_{u(0), u(1), \dots, u(T-1)} J$$

such that $x(t+1) = f(x(t), u(t))$



Linear Quadratic Regulator (LQR)

Given current state $x(0)$

$$\min_{u(0), u(1), \dots, u(T-1)} J$$

Quadratic

Linear

$$\text{such that } x(t+1) = f(x(t), u(t))$$

An optimal feedback law exists.



Linear Quadratic Regulator (LQR)

Given current state $x(0)$

$$\min_{u(0), u(1), \dots, u(T-1)} J$$

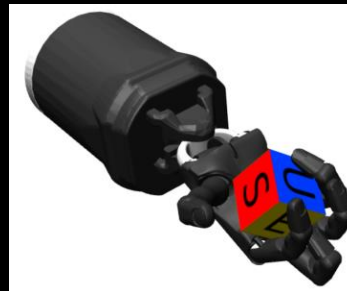
Quadratic

Linear

$$\text{such that } x(t+1) = f(x(t), u(t))$$

But for robotics, dynamics is rarely linear.

Highly non-linear!



An optimal feedback law exists.



Trajectory optimizers in MJPC

- Derivative-based methods

iLQR:

Requires $\frac{\partial f}{\partial x}$, $\frac{\partial f}{\partial u}$, $\frac{\partial c}{\partial x}$, $\frac{\partial c}{\partial u}$, $\frac{\partial^2 c}{\partial x^2}$, $\frac{\partial^2 c}{\partial u^2}$, $\frac{\partial^2 c}{\partial x \partial u}$

Gradient descent:

Requires $\frac{\partial J}{\partial u}$

Derivative computation is expensive!



Trajectory optimizers in MJPC

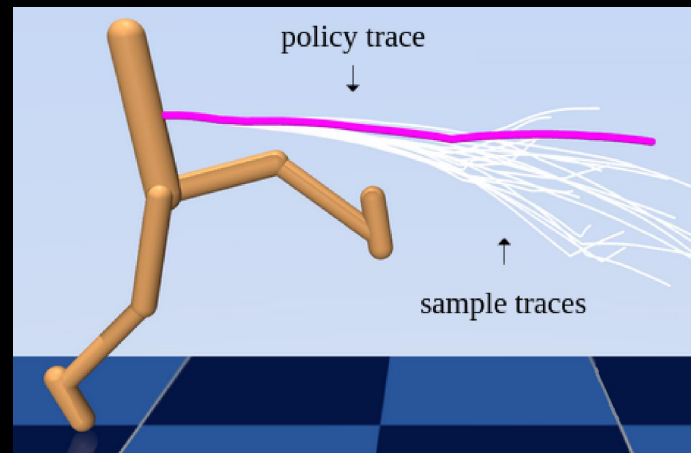
- A derivative-free method

Predictive Sampling Algorithm:

Step 1: Rollout all N noisy trajectories

Step 2: Pick the best one

- Performs surprisingly well!
- Parallelizable!



Feedback Control vs MPC



Feedback control

MPC



Feedback Control vs MPC

Feedback control

- Computationally cheap.

MPC

- Expensive.



Feedback Control vs MPC

Feedback control

- Computationally cheap.
- Reacts to immediate residual.

MPC

- Expensive.
- Longer horizon. But still myopic after horizon T .



Feedback Control vs MPC

Feedback control

- Computationally cheap.
- Reacts to immediate residual.
- Doesn't require a model.

MPC

- Expensive.
- Longer horizon. But still myopic after horizon T .
- Requires a computational model.
 - Sim2Real gap.



Feedback Control vs MPC

Feedback control

- Computationally cheap.
- Reacts to immediate residual.
- Doesn't require a model.
- Limited to regulation/tracking.

MPC

- Expensive.
- Longer horizon. But still myopic after horizon T .
- Requires a computational model.
 - Sim2Real gap.
- Can encode higher-level tasks.

MPC vs Reinforcement Learning



MPC

Reinforcement Learning



MPC vs Reinforcement Learning

MPC

- No offline training.

Reinforcement Learning

- Offline training needed.



MPC vs Reinforcement Learning

MPC

- No offline training.
- Requires a model.

Reinforcement Learning

- Offline training needed.
- Does not require a model.



MPC vs Reinforcement Learning

MPC

- No offline training.
- Requires a model.
- Limited to our state representations.

Reinforcement Learning

- Offline training needed.
- Does not require a model.
- Can discover latent representations, and “intelligent” behavior.



MPC vs Reinforcement Learning

MPC

- No offline training.
- Requires a model.
- Limited to our state representations.
- Slower during execution.

Reinforcement Learning

- Offline training needed.
- Does not require a model.
- Neural network representations and more “intelligent” behavior.
- Learns a policy, a direct mapping from state to action.



Maria College

Part 3: Challenges



What should you expect?

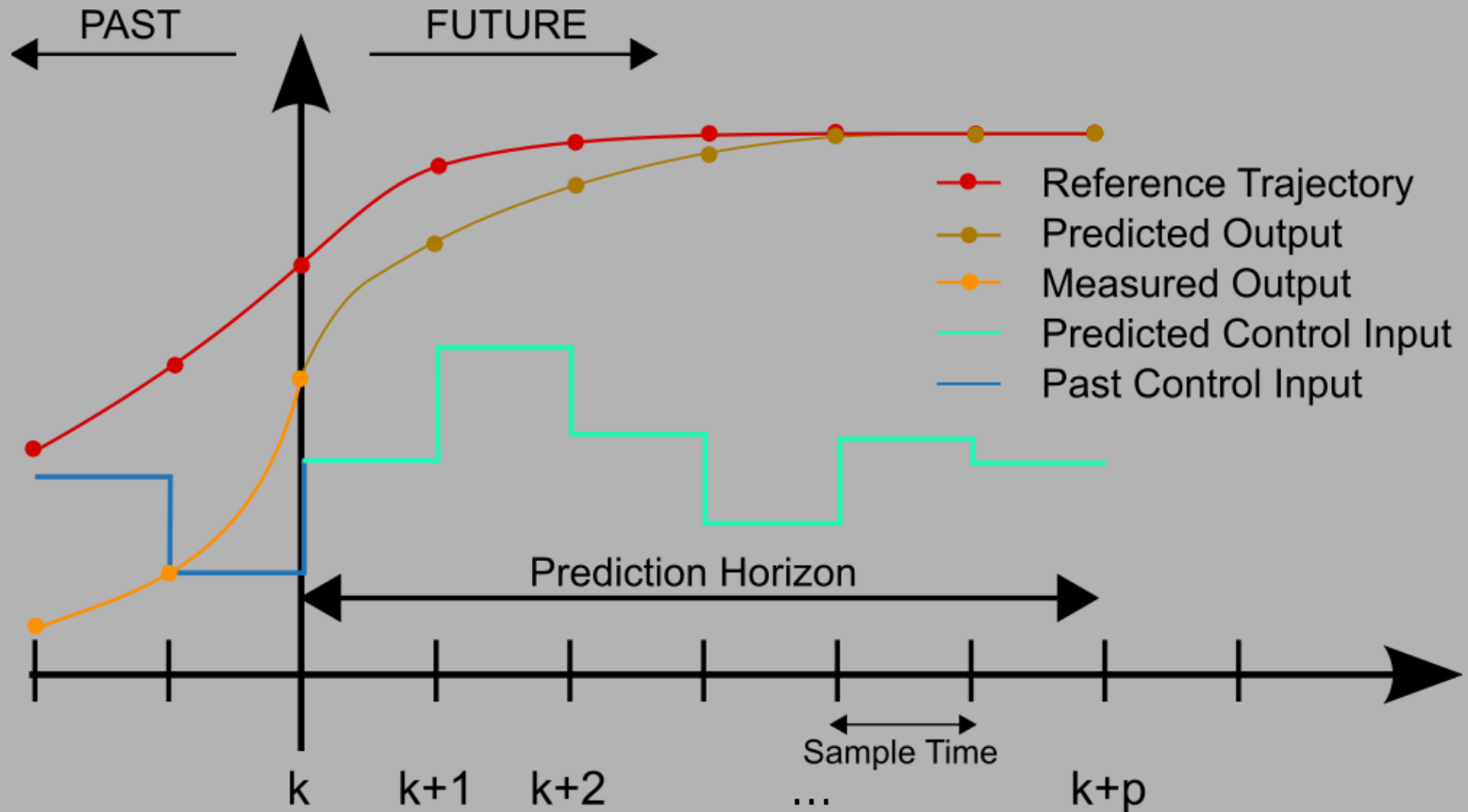
- Uncertainty and Partial Observability
- Long Horizon
- Under/Over actuation
- Sim-to-real gap
- Tendon strain + skin non-linearity
- Encoder's sensibility



Uncertainty and Partial Observability



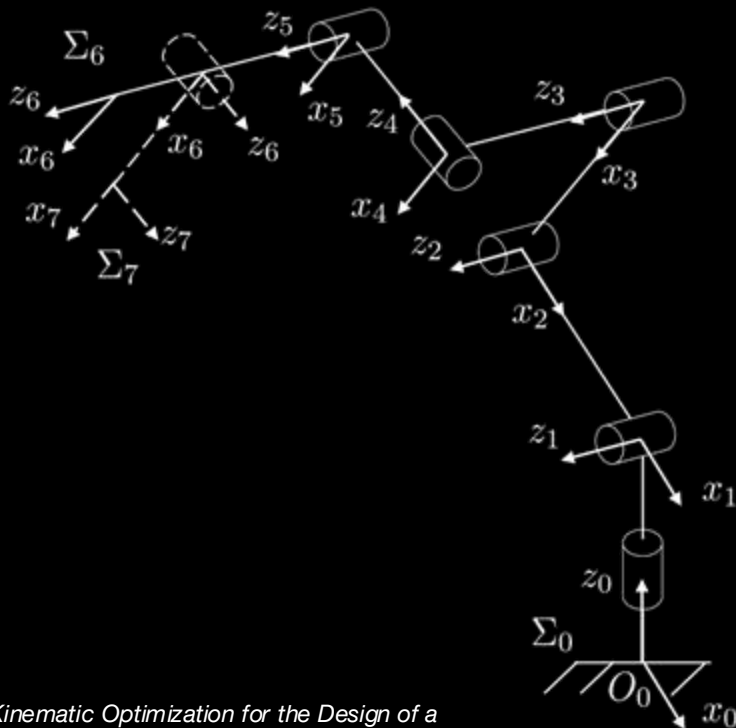
Long Horizon



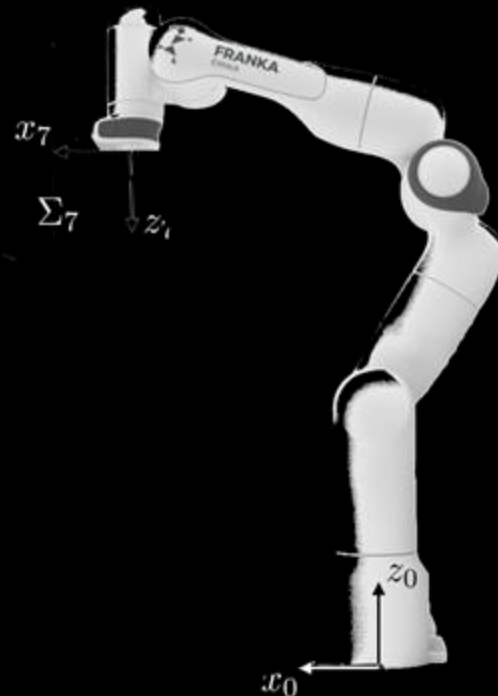
- Reference Trajectory
- Predicted Output
- Measured Output
- Predicted Control Input
- Past Control Input



Underactuation and Overactuation



(a)



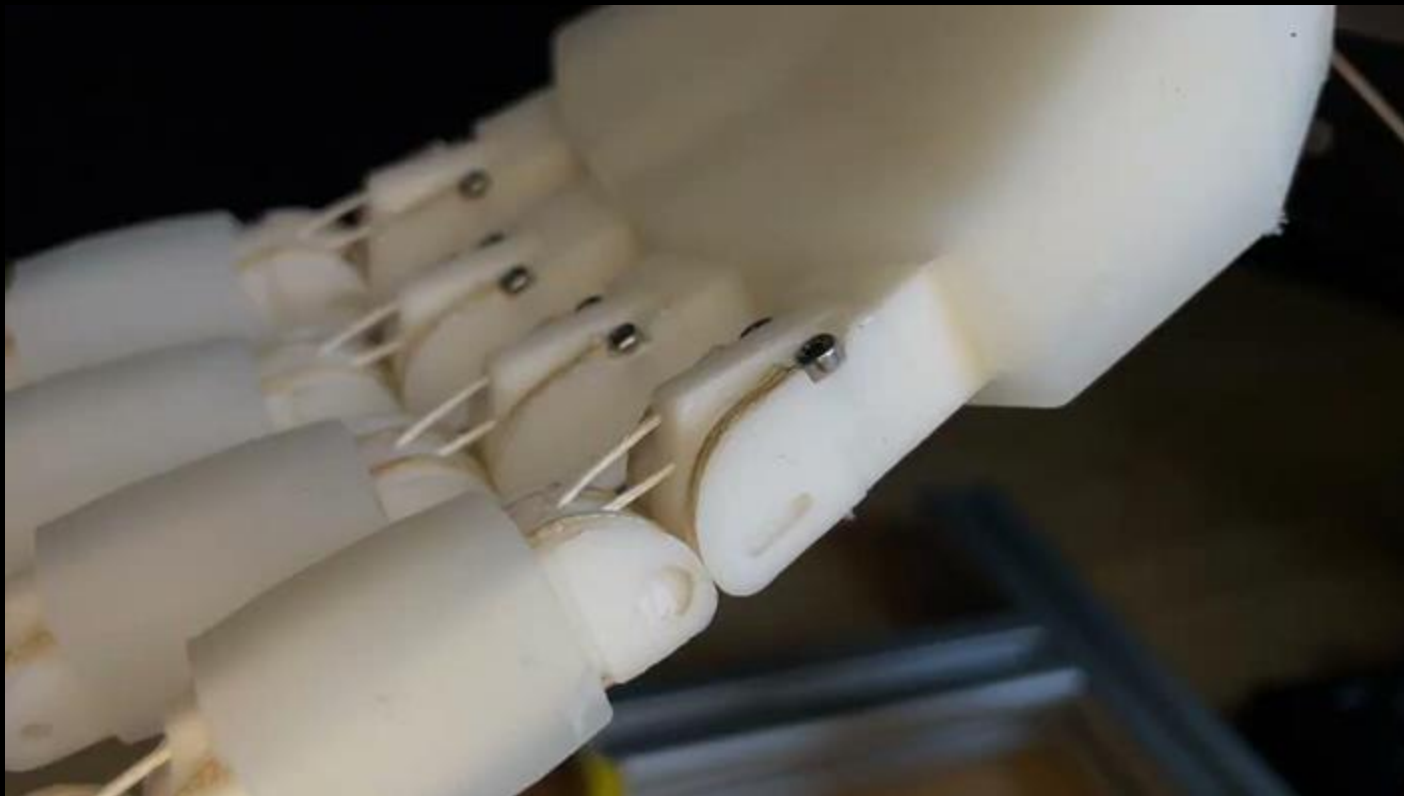
(b)

Filippeschi et al. *Kinematic Optimization for the Design of a Collaborative Robot End-Effector for Tele-Echography* (2021)

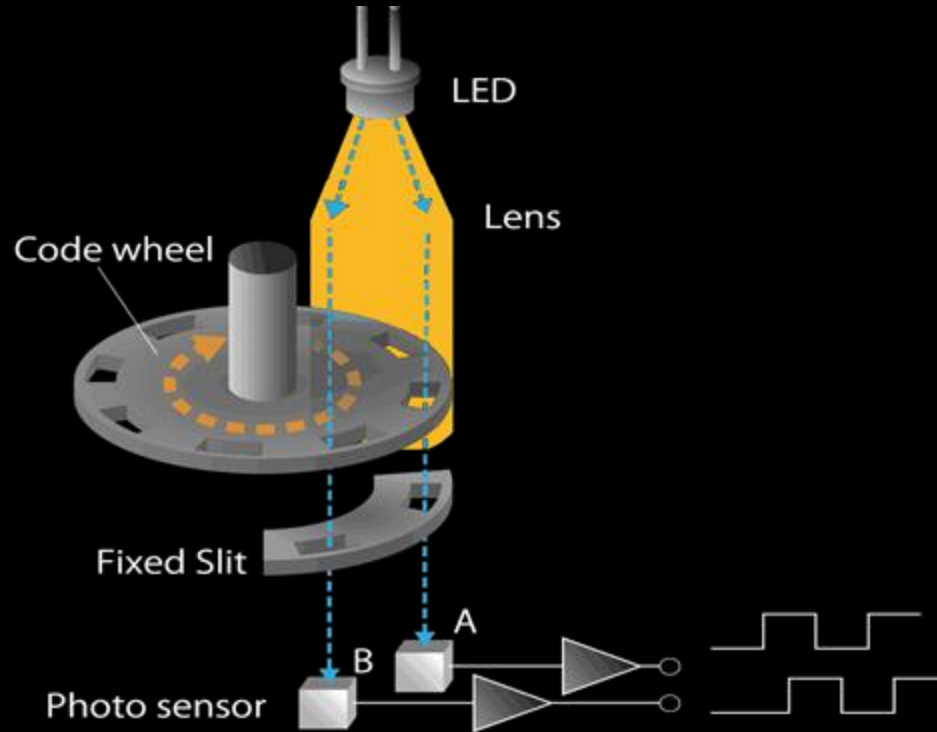
Sim-to-real gap



Tendon strain + skin non-linearity



Encoder's sensibility



Asahi Kasei Microdevices

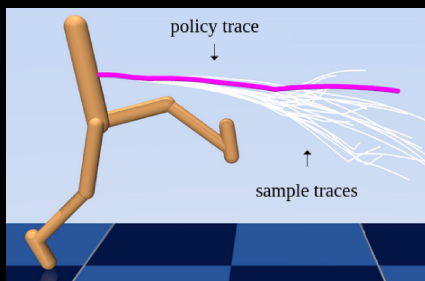


Wrap up

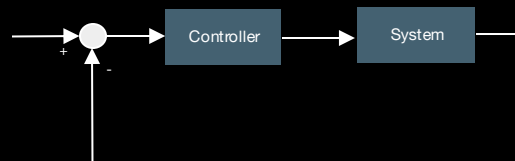
1. Sensing



2b. Model Predictive Control



2a. Feedback Control



3. Challenges



Backup Slides

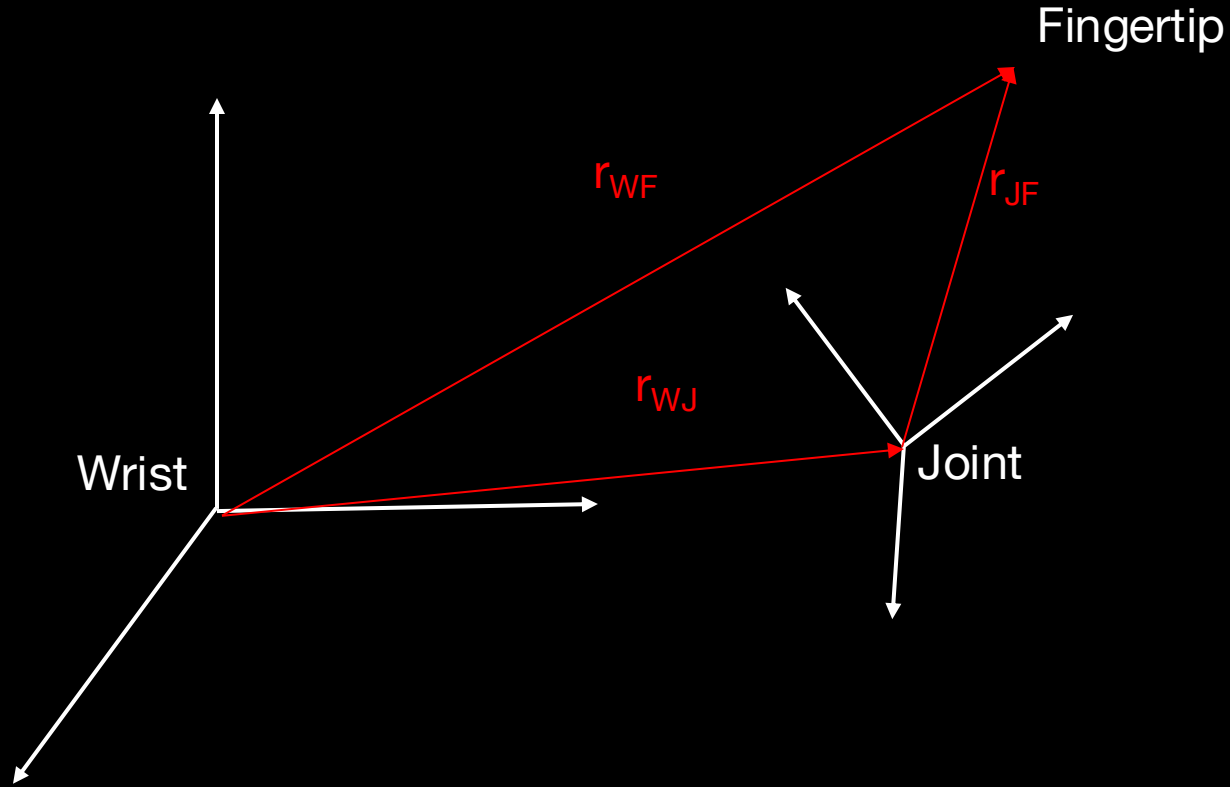
Sensing the pose: two methods



- **Direct** methods: Direct reference to the **world reference frame**
 - The sensors obtain the absolute value of the state we are measuring
- **Indirect** methods: Obtain a measurement with reference to a **second frame**
 - The sensors will estimate a relative measurement that can be transformed into an absolute measurement

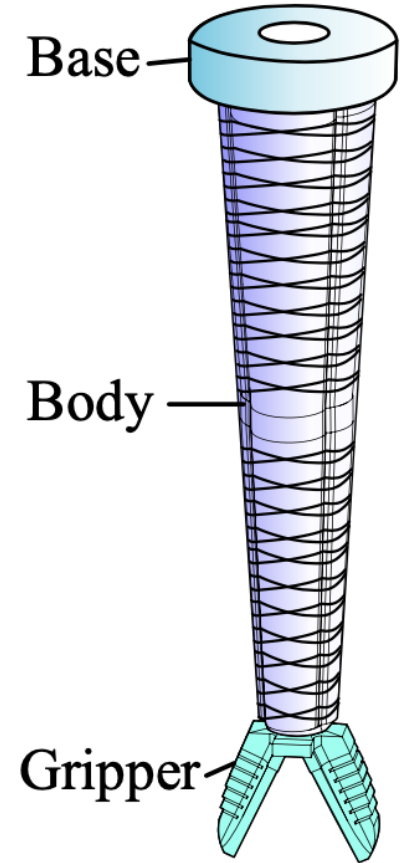
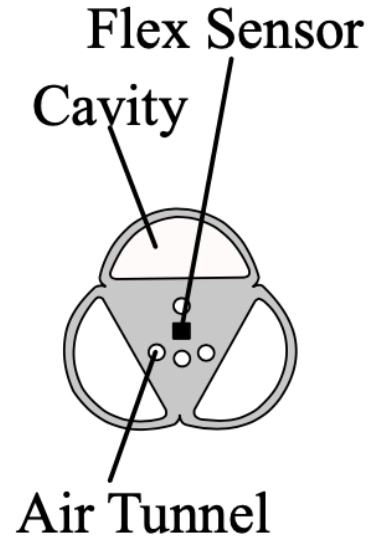
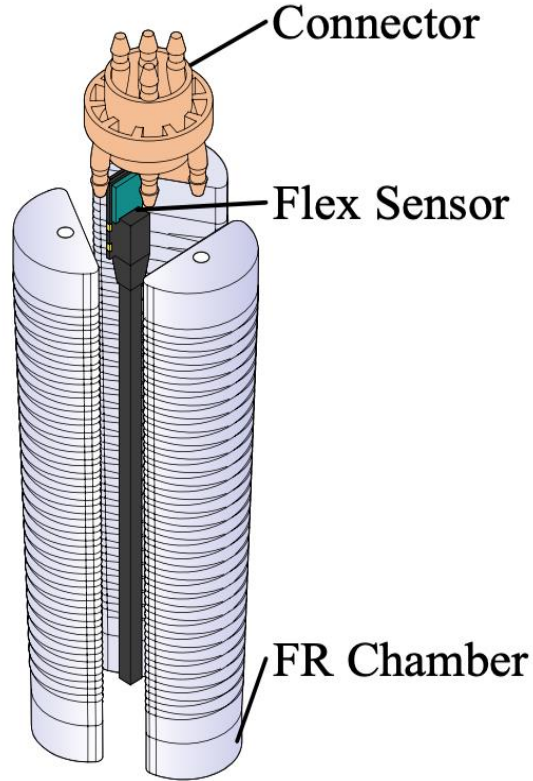


Second solution



Indirect methods

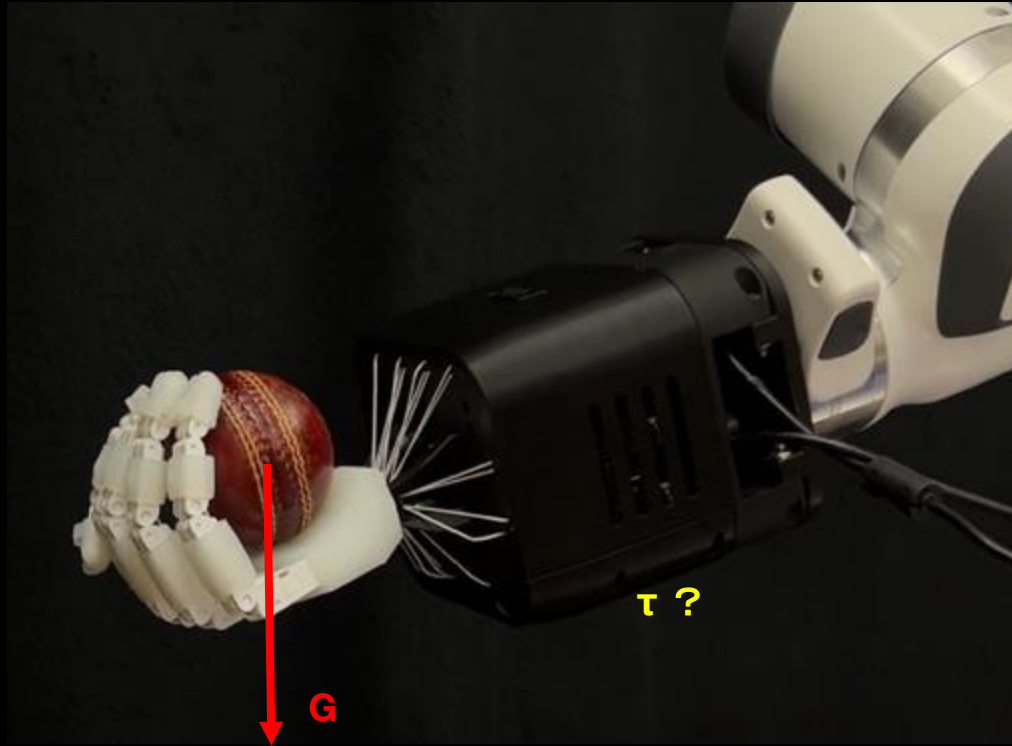
e.g., Built-in Flex Sensor



Toshimitsu, Y., Wong, K. W., Buchner, T., & Katzschmann, R. (2021, September). Sopra: Fabrication & dynamical modeling of a scalable soft continuum robotic arm with integrated proprioceptive sensing. In *2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)* (pp. 653-660). IEEE.



Force control for tendon actuation



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Force control for tendon actuation

Tendon Lengths

$$p = g(l) = g(f(q)) = F(q)$$

Motor Positions

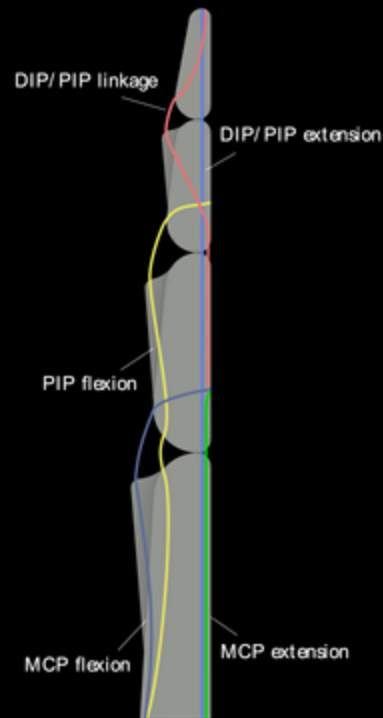
Joint Angles

The diagram illustrates the force control equation for tendon actuation. The equation is $p = g(l) = g(f(q)) = F(q)$. A red arrow points from the text "Tendon Lengths" to the variable l in the equation. Another red arrow points from the text "Motor Positions" to the variable p . A third red arrow points from the text "Joint Angles" to the variable q in the inner function $f(q)$.



Force control for tendon actuation

$$J_m = \begin{bmatrix} \frac{\partial p_1}{\partial q_1} & \frac{\partial p_1}{\partial q_2} \\ \frac{\partial p_2}{\partial q_1} & \frac{\partial p_2}{\partial q_2} \end{bmatrix}$$

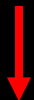


75



Force control for tendon actuation

Velocity of the
finger joints



$$\dot{p} = J_m \cdot \dot{q}$$



Velocity of
the motors

$$\tau^T \cdot \dot{q} = T^T \cdot \dot{p}$$

Conservation of Power



$$\tau^T \cdot \dot{q} = T^T \cdot J_m \cdot \dot{q}$$



$$\tau = J_m^T \cdot T$$

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Force control for tendon actuation

Previous slide: $\tau = J_m^T \cdot T$

$$\dot{X}_{fingertip} = J_{fingertip} \cdot \dot{q}$$

$$\tau^T \cdot \dot{q} = F_{fingertip}^T \cdot \dot{X}_{fingertip}$$

$$\tau^T \cdot \dot{q} = F_{fingertip}^T \cdot J_{fingertip} \cdot \dot{q}$$



$$\tau = J_{fingertip}^T \cdot F_{fingertip}$$

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Force control for tendon actuation

$$\left. \begin{aligned} \tau &= J_m^T \cdot T \\ \tau &= J_{fingertip}^T \cdot F_{fingertip} \end{aligned} \right\} T = (J_m^T)^{-1} \cdot J_{fingertip}^T \cdot F_{fingertip}$$

Outro no slide





Useful links

<https://link.springer.com/book/10.1007/978-3-319-54413-7>

<https://smartlabai.medium.com/a-brief-overview-of-imitation-learning-8a8a75c44a9c>

<https://underactuated.csail.mit.edu/index.html>

<https://www.kalmanfilter.net/default.aspx>